

MATEMATIKA 1: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PIŠITE DVOSTRANO!** Obavezno popuniti sva polja ispod!!

POPUNJAVA
NASTAVNIK
Broj ↓
bodova

C7

IME I PREZIME: Mateja Čulina

BROJ INDEKSA: 17-2-0206-2012

ZAOKRUŽITI AKO ŽELITE: ustmeni kod prof. Uglešića

Među kompleksnim brojevima odrediti rješenja jednadžbe $z^3 = -(-i)^{886}$. Prikazati rješenja u kompleksnoj ravni!

Riješi sustav Gaussovom metodom i obavezno provjeri rješenje:

$$\begin{aligned} 5x + 4z + 2t &= 3 \\ x - y + 2z + t &= 1 \\ 4x + y + 2z &= 1 \\ x + y + z + t &= 0 \end{aligned}$$

3. Odrediti kada je $\frac{x+1}{\sqrt{x^2-x}} - 1 > 0$. Obavezno uvrštavanjem provjeriti rješenje jednadžbi koje se javljaju tokom rješavanja nejednadžbe.

13+2

Za funkciju: $f(x) = \sqrt{x^2 + 8x + 5}$ treba:

- (a) pronaći drugu derivaciju
(b) na temelju ispitivanja toka funkcije skicirati graf

5. Odrediti i provjeriti rješenje $\lim_{x \rightarrow +\infty} \left(\frac{n}{n-4}\right)^n =$

8+2

6. Riješiti jednadžbu $\log_{10} x = \arctan x$ grafičkom metodom. *Provjeriti uvrštavanjem!*

10+5

Ukupno:

~~10~~
~~20(graf)~~
~~8+2~~
~~10+5~~

4. $f(x) = \sqrt{x^2 + 8x + 5}$

a) druga derivacija

$$\begin{aligned} f'(x) &= \left((x^2 + 8x + 5)^{\frac{1}{2}} \right)' \\ &= \frac{1}{2} (x^2 + 8x + 5)^{-\frac{1}{2}} \cdot (2x + 8) \\ &= \frac{1}{2} (x^2 + 8x + 5)^{-\frac{1}{2}} \cdot (2x + 8) \quad \checkmark \end{aligned}$$

$$f''(x) = -\frac{1}{4} (x^2 + 8x + 5)^{-\frac{3}{2}} \cdot (2x + 8) \cdot 2 \quad \times$$

$$= -\frac{1}{2} (x^2 + 8x + 5)^{-\frac{3}{2}} (2x + 8)$$

b) 1. domena

$$x^2 + 8x + 5 \geq 0$$

$$dx^2 + 5 \geq 0$$

$$dx^2 \geq 5 / 2$$

$$dx \geq \sqrt{5} / 2$$

$$x \geq \frac{\sqrt{5}}{2}$$

$$x \geq 0.24$$

$$x_1 = 0.24$$

$$x_2 = -0.24$$

$$Df = (-\infty, -0.24) \cup (-0.24, 0.24) \cup$$

$$(0.24, +\infty)$$

GRAF?

~~Ukupno: 10+5+8+2+10+5=40~~

2. ZADATK

$$5x + 4z + 2t = 3$$

$$x - y + 2z + t = 1$$

$$4x + y + 2z = 1$$

$$x + y + z + t = 0$$

$$\begin{bmatrix} 5 & 0 & 4 & 2 & | & 3 \\ 1 & -1 & 2 & 1 & | & 1 \\ 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 0 & 4 & 2 & | & 3 \\ 1 & -1 & 2 & 1 & | & 1 \\ 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 0 & 4 & 2 & | & 3 \\ 2 & 0 & 3 & 2 & | & 1 \\ 4 & 1 & 0 & 2 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 0 & 4 & 2 & | & 3 \\ 0 & -2 & 1 & 0 & | & 1 \\ 0 & -3 & -4 & -2 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 0 & 4 & 2 & | & 1 \\ 0 & 2 & 1 & 0 & | & 1 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 2 & 1 & 0 & | & 1 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 5 & 0 & 4 & 2 & | & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & -2 & 1 & 0 & | & 1 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & -5 & 1 & 2 & | & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & -2 & 1 & 0 & | & 1 \\ 0 & -5 & 0 & 2 & | & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 2 & 1 & 0 & | & 1 \\ 0 & 1 & 0 & 3 & | & \frac{1}{3} \\ 0 & -5 & 1 & 2 & | & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & 1 & \frac{1}{3} & 0 & | & -\frac{1}{2} \\ 0 & 0 & \frac{13}{2} & -2 & | & \frac{1}{2} \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & 0 & 1 & 0 & | & \frac{5}{3} \\ 0 & 0 & \frac{13}{2} & 2 & | & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & 0 & 1 & 0 & | & \frac{5}{3} \\ 0 & 0 & 1 & 1 & | & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & 0 & 1 & 0 & | & \frac{5}{3} \\ 0 & 0 & -2 & 1 & | & -4 \end{bmatrix}$$

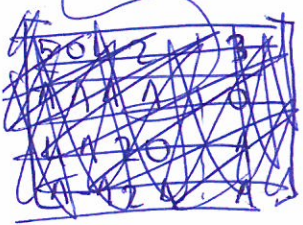
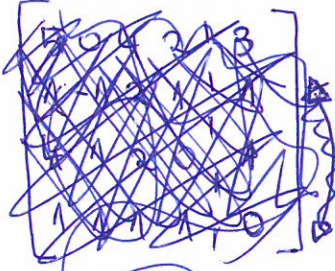
$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & 0 & 1 & 0 & | & \frac{5}{3} \\ 0 & 0 & 1 & 1 & | & 2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & 0 & 1 & -2 & | & 2 \\ 0 & 0 & 1 & 0 & | & \frac{5}{3} \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & | & 0 \\ 0 & 1 & \frac{4}{3} & \frac{1}{3} & | & \frac{1}{3} \\ 0 & 0 & 1 & -2 & | & 2 \\ 0 & 0 & 0 & -2 & | & 12 \end{bmatrix}$$

$$\begin{aligned} x + y + z + t &= 0 \\ y + \frac{4}{3}z + \frac{1}{3}t &= \frac{1}{3} \\ z - 2t &= 2 \\ -2t &= 2 \end{aligned}$$

$$t = -1$$



$$x + \frac{8}{33} + \frac{5}{11} + \frac{17}{22} = 0$$

$$x + \frac{16 + 30 - 51}{66} = 0$$

$$x + \frac{5}{66} = 0$$

$$x + \frac{-5}{66} = 0$$

$$x = \frac{5}{66}$$

VIDI RADAS

IME I PREZIME: Matea Culina

BROJ INDEKSA: 17-2-0206-2012

1.) $z^3 = -(-i)^{896}$

$z^3 = -(-i)^2$

~~$z^3 = -(2)^2$~~ \times

$z^3 = -4 \mid^3$

$z = \sqrt[3]{-4}$

$|z| = r = \sqrt{x^2 + y^2} = \sqrt{(-4)^2 + 0^2}$
 $= \sqrt{16}$
 $= 4$

$\operatorname{tg} \rho = \frac{y}{x}$

$= \frac{0}{-4}$

$\rho = 0^\circ$

$360^\circ - \rho = 360^\circ$

$x = -4$

$y = 0$

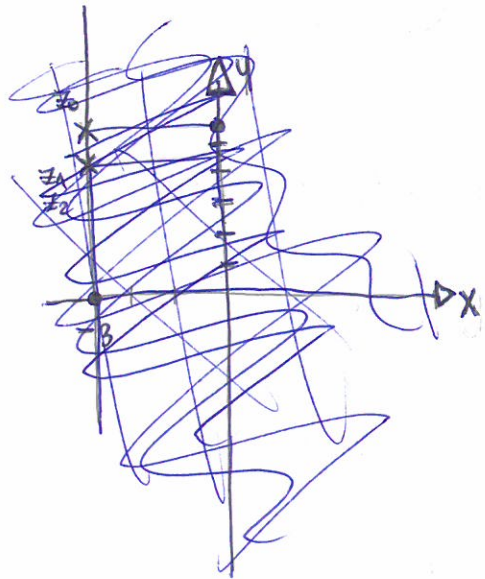
$n = 3$

$m = 4$

$\varphi = 360^\circ$

17A

~~$k=0$
 $z = \sqrt[3]{-4} \left(\cos \frac{r \cdot (k+360^\circ)}{n} + i \sin \frac{k+360^\circ}{n} \right)$
 $z = \sqrt[3]{-4} \left(\cos \frac{0+360^\circ}{3} + i \sin \frac{0+360^\circ}{3} \right)$
 $z = 6 \left(\cos 120 + i \sin 120 \right)$
 $z = 6 \left(-\frac{1}{2} + \frac{\sqrt{3}}{2}i \right)$
 $z_0 = (-3) + 5.19i$
 $x \quad y$~~



~~$k=1$
 $z = 6 \left(\cos \frac{1+360^\circ}{3} + i \sin \frac{1+360^\circ}{3} \right)$
 $z = 6 \left(\cos 120.3 + i \sin 120.3 \right)$
 $z = 6 \left(-0.5 + 0.8i \right)$
 $z_1 = (-3) + 4.8i$
 $x \quad y$~~

~~$k=1$
 $z = 6 \left(\cos \frac{4+1+360}{3} + i \sin \dots \right)$~~



~~$k=2$
 $z = 6 \left(\cos \frac{2+360^\circ}{3} + i \sin \frac{2+360^\circ}{3} \right)$
 $z = 6 \left(-0.5 + 0.8i \right)$
 $z_2 = (-3) + 4.8i$
 $x \quad y$~~

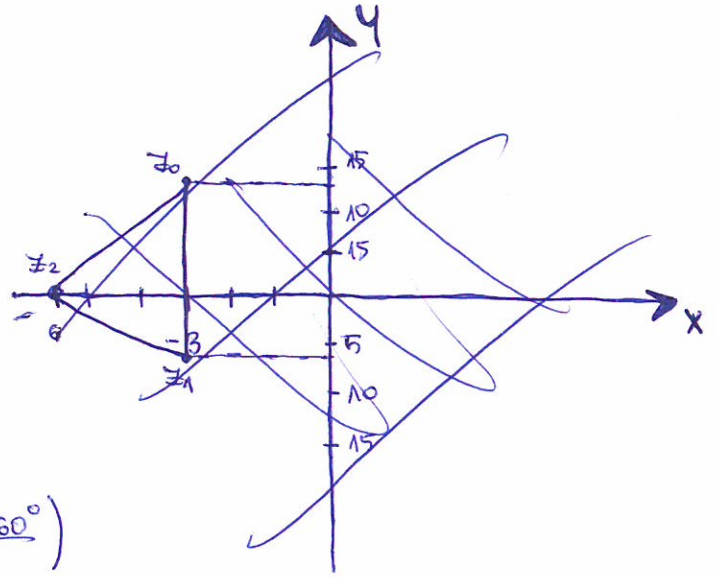
~~scribbles~~

$$k=0$$

$$z_0 = 6(\cos 120 + i \sin 120)$$

$$= 6(-0.5 + 0.86i)$$

$$= \underbrace{-3}_x + \underbrace{+14.6}_y i$$



$$z = \sqrt[n]{r} \left(\cos \frac{360 \cdot k + \theta}{n} + i \sin \frac{360 \cdot k + \theta}{n} \right)$$

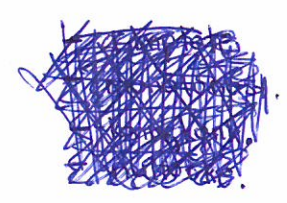
$$k=1$$

$$z_1 = 3\sqrt[4]{4} \left(\cos \frac{360 \cdot 1 + 360^\circ}{3} + i \sin \frac{360 \cdot 1 + 360^\circ}{3} \right)$$

$$= 6(\cos 240 + i \sin 240)$$

$$= 6(-0.5 - 0.86i)$$

$$= \underbrace{-3}_x \underbrace{-5.1}_y i$$



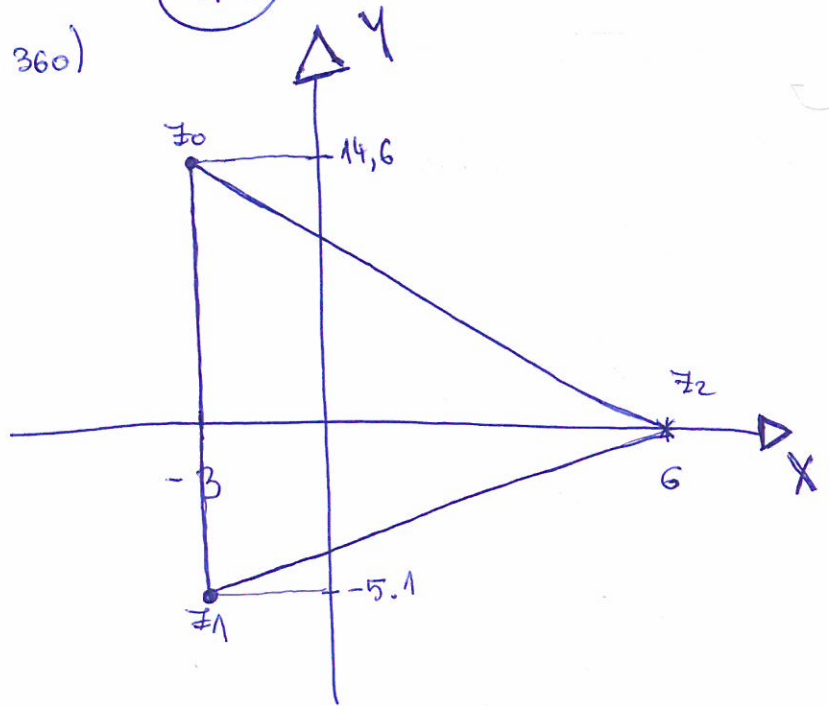
$$k=2$$

$$z_2 = \sqrt[n]{r} \left(\cos 360 + i \sin 360 \right)$$

$$= 6(1 + 0i)$$

$$= \underbrace{6}_x + \underbrace{0}_y i$$

GRAF



scribble

MATEMATIKA 1: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PIŠITE DVOSTRANO!** Obavezno popuniti sva polja ispod!!

POPUNJAVA
NASTAVNIK
Broj ↓
bodova

IME I PREZIME: **MATE RADAŠ**

BROJ INDEKSA: **17-2-0183-2012**

ZAOKRUŽITI AKO ŽELITE: ustmeni kod prof. Uglešića

C7

1. Među kompleksnim brojevima odrediti rješenja jednadžbe $z^3 = -(-i)^{886}$. Prikazati rješenja u kompleksnoj ravni! 10+5
2. Riješi sustav Gaussovom metodom i obavezno provjeri rješenje: 10+5

$$\begin{aligned} 5x + 4z + 2t &= 3 \\ x - y + 2z + t &= 1 \\ 4x + y + 2z &= 1 \\ x + y + z + t &= 0 \end{aligned}$$
3. Odrediti kada je $\frac{x+1}{\sqrt{x^2-x}} - 1 > 0$. Obavezno uvrštavanjem provjeriti rješenje jednadžbi koje se javljaju tokom rješavanja nejednadžbe. 13+2
4. Za funkciju: $f(x) = \sqrt{x^2 + 8x + 5}$ treba:
 - (a) pronaći drugu derivaciju 10
 - (b) na temelju ispitivanja toka funkcije skicirati graf 20(graf)
5. Odrediti i provjeriti rješenje $\lim_{x \rightarrow +\infty} \left(\frac{n}{n-4}\right)^n =$ 8+2
6. Riješiti jednadžbu $\log_{10} x = \arctan x$ grafičkom metodom. *Provjeriti uvrštavanjem!* 10+5

Ukupno:
48

2.)
$$\begin{aligned} 5x + 4z + 2t &= 3 \\ x - y + 2z + t &= 1 \\ 4x + y + 2z &= 1 \\ x + y + z + t &= 0 \end{aligned}$$

$$\begin{array}{cccc|c} x & y & z & t & \\ \hline 5 & 0 & 4 & 2 & 3 \\ 1 & -1 & 2 & 1 & 1 \\ 4 & 1 & 2 & 0 & 1 \\ 1 & 1 & 1 & 1 & 0 \end{array} \xrightarrow{1.A. \leftrightarrow 4.A.} \begin{array}{cccc|c} 1 & -1 & 2 & 1 & 0 \\ 1 & -1 & 2 & 1 & 1 \\ 4 & 1 & 2 & 0 & 1 \\ 5 & 0 & 4 & 2 & 3 \end{array}$$

$\left. \begin{array}{l} 2.A. - 1.A. \\ 3.A. - 4 \times 1.A. \\ 4.A. - 5 \times 1.A. \end{array} \right\}$

$$\sim \begin{array}{cccc|c} 1 & -1 & 2 & 1 & 0 \\ 0 & -2 & 0 & 0 & 1 \\ 0 & -3 & -2 & -4 & 1 \\ 0 & -5 & -1 & -3 & 3 \end{array} \xrightarrow{2.A. - 3.A.} \begin{array}{cccc|c} 1 & -1 & 2 & 1 & 0 \\ 0 & 1 & 3 & 4 & -1 \\ 0 & -3 & -2 & -4 & 1 \\ 0 & -5 & -1 & -3 & 3 \end{array}$$

$\left. \begin{array}{l} 1.A. - 2.A. \\ 3.A. + 3 \times 2.A. \\ 4.A. + 5 \times 2.A. \end{array} \right\}$

$$\left[\begin{array}{cccc|c} 1 & 0 & -2 & -3 & 0 \\ 0 & -1 & 3 & -4 & 0 \\ 0 & 0 & 7 & 8 & 1 \\ 0 & 0 & 14 & -17 & -3 \end{array} \right] \xrightarrow{4 \cdot \pi - 2 \times 3 \cdot \pi} \left[\begin{array}{cccc|c} -1 & 0 & -2 & -3 & 0 \\ 0 & -1 & 3 & -4 & 0 \\ 0 & 0 & 7 & 8 & 1 \\ 0 & 0 & 0 & 1 & 1 \end{array} \right] \left[\begin{array}{cccc|c} -1 & 0 & -2 & -3 & 0 \\ 0 & -1 & 3 & -4 & 0 \\ 0 & 0 & 7 & 8 & 1 \\ 0 & 0 & 0 & 1 & 1 \end{array} \right]$$

$$\begin{aligned} X - 2z - 3t = 0 & \Rightarrow X - 2 \cdot (-1) - 3 \cdot 1 = 0 \Rightarrow X + 2 - 3 = 0 \Rightarrow X = 1 // \\ Y + 3z + 4t = 0 & \Rightarrow Y + 3 \cdot (-1) + 4 \cdot 1 = 0 \Rightarrow Y - 3 + 4 = 0 \Rightarrow Y = -1 // \\ 7z + 8t = 1 & \Rightarrow 7z + 8 \cdot 1 = 1 \Rightarrow 7z = -7 \quad | : 7 \Rightarrow z = -1 // \\ t & = 1 // \end{aligned}$$

PROVJERA:

$$\begin{aligned} 5x + 4z + 2t = 3 & \Rightarrow 5 \cdot 1 + 4 \cdot (-1) + 2 \cdot 1 = 3 \Rightarrow 3 = 3 // \\ x - y + 2z + t = 1 & \Rightarrow 1 - (-1) + 2 \cdot (-1) + 1 = 1 \Rightarrow 2 - 2 + 1 = 1 // \\ 4x + y + 2z = 1 & \Rightarrow 4 \cdot 1 + (-1) + 2 \cdot (-1) = 1 \Rightarrow 4 - 3 = 1 \Rightarrow 1 = 1 // \\ x + y + 2t = 0 & \Rightarrow 1 - 1 - 1 + 1 = 0 \Rightarrow 0 = 0 // \end{aligned}$$



1.)

$$z^3 = -(-i)^{886}$$

$$886 : 4 = 221$$

$$z^3 = -(i^2) \checkmark$$

2/1

$$z^3 = -(\sqrt{-1})^2$$

$$r = \sqrt{x^2 + y^2} \quad \arg z = \frac{y}{x} = \frac{0}{1} = 0$$

$$z^3 = 1 \checkmark / \sqrt[3]{1}$$

$$r = \sqrt{1^2 + 0^2}$$

$$\arg z = 0 \checkmark$$

$$z = \sqrt[3]{1} = 1$$

$$r = 1 \checkmark$$

l=0

$$z_l = \sqrt[m]{r} \left(\cos \frac{\varphi + 2l\pi}{m} + i \sin \frac{\varphi + 2l\pi}{m} \right)$$

l=0

$$z_0 = \sqrt[3]{1} \left(\cos \frac{0 + 2 \cdot 0 \cdot \pi}{3} + i \sin \frac{0 + 2 \cdot 0 \cdot \pi}{3} \right)$$

$$z_0 = 1 (\cos 0 + i \sin 0)$$

$$z_0 = 1$$

l=1

$$z_1 = 1 \left(\cos \frac{0 + 2 \cdot 1 \cdot \pi}{3} + i \sin \frac{0 + 2 \cdot 1 \cdot \pi}{3} \right)$$

$$z_1 = 1 \left(\cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3} \right)$$

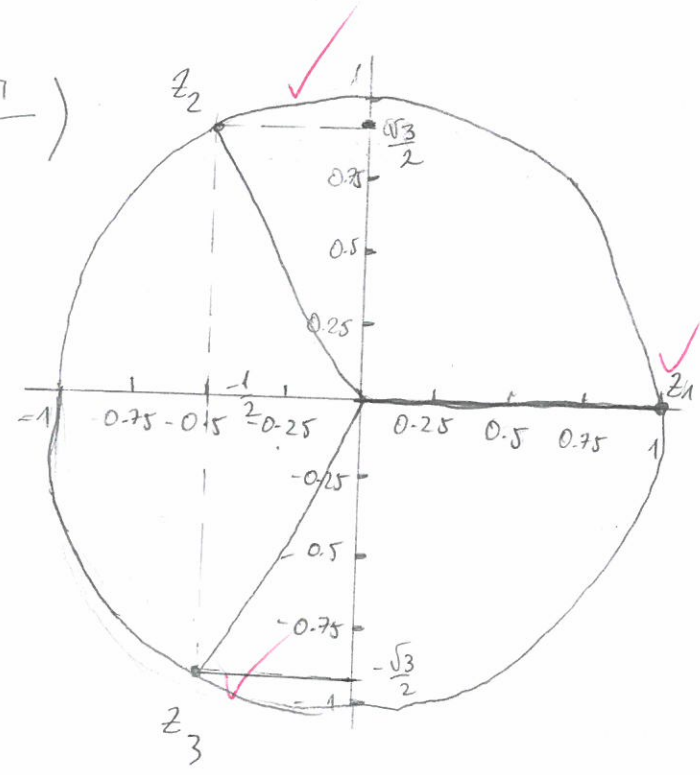
$$z_1 = (\cos 120^\circ + i \sin 120^\circ) = -\frac{1}{2} + \frac{\sqrt{3}}{2} i$$

l=2

$$z_2 = 1 \left(\cos \frac{0 + 2 \cdot 2 \cdot \pi}{3} + i \sin \frac{0 + 2 \cdot 2 \cdot \pi}{3} \right)$$

$$z_2 = \left(\cos \frac{4\pi}{3} + i \sin \frac{4\pi}{3} \right)$$

$$z_2 = \cos 240^\circ + i \sin 240^\circ = -\frac{1}{2} - \frac{\sqrt{3}}{2} i$$



$$3) \frac{x+1}{\sqrt{x^2-x}} - 1 > 0$$

$$x+1=0$$

$$x=-1$$

$$\frac{x+1}{\sqrt{x^2-x}} > 1 > 0$$

$$\sqrt{x^2-x} > 0 / ^2$$

$$x^2-x \neq 0$$

$$x^2-x > 0$$

$$x^2-x \neq 0$$

$$x(x-1) > 0 / :x$$

$$x(x-1) \neq 0$$

$$x > 0$$

$$x_1 \neq 0 \quad \checkmark$$

$$x > 1$$

$$x_2 \neq 1 \quad \checkmark$$

$$x \in (-1, 0) \cup (1, +\infty)$$

TREBALO JE
RADITI TABLICU

ZA

$$f(x) = \frac{x+1-\sqrt{x^2-x}}{\sqrt{x^2-x}}$$

MULTIČIENE
I V.A.

NIJE MULTIČIENE

| | $-\infty$ | -1 | 0 | 1 | $+\infty$ |
|----------------|-----------|------|-----|-----|-----------|
| $\sqrt{x^2-x}$ | + | + | 0 | - | + |
| x^2-x | - | + | + | + | + |
| $x+1$ | - | + | - | + | + |

PROVJERA: $x = -2$

$$\frac{-2+1}{\sqrt{2^2-2}} - 1 > 0$$

$$\frac{-1}{\sqrt{4-2}} - 1 > 0$$

$$\frac{-1}{\sqrt{2}} - 1 > 0$$

$$\frac{-1}{\sqrt{2}} - 1 > 0$$

$$\frac{-1-\sqrt{2}}{\sqrt{2}} > 0$$

$$-1-\sqrt{2} > 0$$

$$-1 > 0$$

IME I PREZIME: MATE RADAŠ

BROJ INDEKSA: 17-2-0183-2012

$$\begin{aligned} 5. \lim_{x \rightarrow +\infty} \left(\frac{x}{x-4} \right)^x &= \lim_{x \rightarrow +\infty} \left(1 + \frac{x}{x-4} - 1 \right)^x = \lim_{x \rightarrow +\infty} \left(1 + \frac{x-x-4}{x-4} \right)^x = \\ &= \lim_{x \rightarrow +\infty} \left(1 + \frac{-4}{x-4} \right)^x = \lim_{x \rightarrow +\infty} \left(1 + \frac{\frac{1}{\frac{1}{x-4}}}{-4} \right)^x = \lim_{x \rightarrow +\infty} \left(1 + \frac{1}{\frac{x-4}{-4}} \right)^{\frac{x-4}{-4} \cdot \frac{-4x}{x-4}} = \\ &= e^{\lim_{x \rightarrow +\infty} \frac{-4x}{x-4}} = \lim_{x \rightarrow +\infty} \frac{-4}{1} = -4 \quad \checkmark \end{aligned}$$

PROVJERA:

$$\left(\frac{10}{10-4} \right)^{10} = \dots$$

$$\left(\frac{100}{100-4} \right)^{100} = \dots$$

$$\left(\frac{1000}{1000-4} \right)^{1000} = \dots$$

$$e^{-4} = \dots$$

PA

LI

SE

PRIBLIŽAVA

LIMESU?

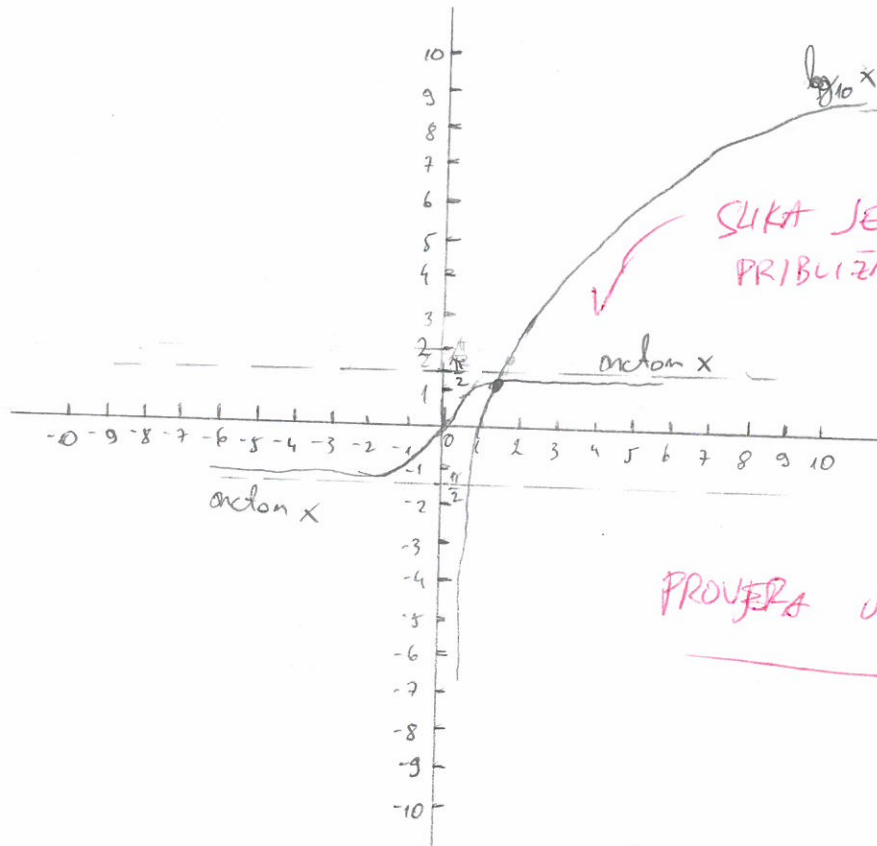
4.) $f(x) = \sqrt{x^2 + 8x + 5}$

a) $f'(x) = (\sqrt{x^2 + 8x + 5})' = (\sqrt{x^2})' + (\sqrt{8x})' + (\sqrt{5})' = 1 + (8x^{\frac{1}{2}})' + 0 =$
 $= 1 + \frac{1}{2} \cdot 4x^{-\frac{1}{2}} = 1 + \frac{1}{\sqrt{4x}} = 1 + \frac{1}{2\sqrt{x}} = (1 + (2\sqrt{x})^{-1})' = 0 - (2\sqrt{x})^{-2} =$
 $f'(x) = \frac{1}{4x}$

b.)

6.) $\log_{10} x = \arctan x$

$x \approx 1.1$



SIKA JE PRIBLIŽNO TOČNA.

PROVERA UVRŠTAVANJE

MATEMATIKA 1: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PIŠITE DVOSTRANO!** Obavezno popuniti sva polja ispod!!

POPUNJAVA
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Broj ↓
bodova

IME I PREZIME: ŠIME-BORNA MAGAŠ BROJ INDEKSA: 17-2-0108-2011

ZAOKRUŽITI AKO ŽELITE: ustmeni kod prof. Uglešića

C7

1. Među kompleksnim brojevima odrediti rješenja jednadžbe $z^3 = -(-i)^{886}$. Prikazati rješenja u kompleksnoj ravni!

10+5

2. Riješi sustav Gaussovom metodom i obavezno provjeri rješenje:

10+5

$$\begin{aligned} 5x + 4z + 2t &= 3 \\ x - y + 2z + t &= 1 \\ 4x + y + 2z &= 1 \\ x + y + z + t &= 0 \end{aligned}$$

3. Odrediti kada je $\frac{x+1}{\sqrt{x^2-x}} - 1 > 0$. Obavezno uvrštavanjem provjeriti rješenje jednadžbi koje se javljaju tokom rješavanja nejednadžbe.

13+2

4. Za funkciju: $f(x) = \sqrt{x^2 + 8x + 5}$ treba:

(a) pronaći drugu derivaciju

10

(b) na temelju ispitivanja toka funkcije skicirati graf

20(graf)

5. Odrediti i provjeriti rješenje $\lim_{x \rightarrow +\infty} \left(\frac{n}{n-4}\right)^n =$

8+2

6. Riješiti jednadžbu $\log_{10} x = \arctan x$ grafičkom metodom. Provjeriti uvrštavanjem!

10+5

2) $5x + 4z + 2t = 3$
 $x - y + 2z + t = 1$
 $4x + y + 2z = 1$
 $x + y + z + t = 0$

$$\left[\begin{array}{cccc|c} 5 & 0 & 4 & 2 & 3 \\ 1 & -1 & 2 & 1 & 1 \\ 4 & 1 & 2 & 0 & 1 \\ 1 & 1 & 1 & 1 & 0 \end{array} \right] \sim \left[\begin{array}{cccc|c} 1 & 0 & 4/5 & 2/5 & 3/5 \\ 1 & -1 & 2 & 1 & 1 \\ 4 & 1 & 2 & 0 & 1 \\ 1 & 1 & 1 & 1 & 0 \end{array} \right]$$

Ukupno: ~~$R_2 - R_1$~~
 ~~$R_3 - 4R_1$~~
 ~~$R_4 - R_1$~~

$$\sim \left[\begin{array}{cccc|c} 1 & 0 & 4/5 & 2/5 & 3/5 \\ 0 & -1 & 6/5 & 3/5 & 2/5 \\ 0 & 1 & -6/5 & 8/5 & -7/5 \\ 0 & 1 & 1/5 & 3/5 & -3/5 \end{array} \right] \cdot (-1) \sim \left[\begin{array}{cccc|c} 1 & 0 & 4/5 & 2/5 & 3/5 \\ 0 & 1 & -6/5 & -3/5 & -2/5 \\ 0 & 1 & -6/5 & 8/5 & -7/5 \\ 0 & 1 & 1/5 & 3/5 & -3/5 \end{array} \right]$$

$$\sim \left[\begin{array}{cccc|c} 1 & 0 & 4/5 & 2/5 & 3/5 \\ 0 & 1 & -6/5 & -3/5 & -2/5 \\ 0 & 0 & 11/5 & -1 & -1 \\ 0 & 0 & 7/5 & 6/5 & -1/5 \end{array} \right]$$

~~$R_3 - R_2$~~
 ~~$R_4 - R_2$~~

nema rješenja! ~~X~~

$$4) f(x) = \sqrt{x^2 + 8x + 5}$$

$$f'(x) = (\sqrt{x^2 + 8x + 5})' = (\sqrt{5 + x^2 + 8 \cdot x})' = \frac{1}{2} \cdot (5 + x^2 + 8 \cdot x)'$$

$$\cdot (\sqrt{5 + x^2 + 8 \cdot x})^{-1} = \frac{1}{2} \cdot \frac{(5 + x^2 + 8 \cdot x)'}{\sqrt{5 + x^2 + 8 \cdot x}} = \frac{1}{2} \cdot \frac{(5)' + (x^2 + 8 \cdot x)'}{\sqrt{5 + x^2 + 8 \cdot x}} =$$

$$= \frac{1}{2} \cdot \frac{0 + (x^2)' + (8 \cdot x)'}{\sqrt{5 + x^2 + 8 \cdot x}} = \frac{1}{2} \cdot \frac{(x^2)' + (8 \cdot x)'}{\sqrt{5 + x^2 + 8 \cdot x}} =$$

$$= \frac{1}{2} \cdot \frac{2 \cdot 1 \cdot x + 8 \cdot 1}{\sqrt{5 + x^2 + 8 \cdot x}} = \frac{1}{2} \cdot \frac{8 + 2 \cdot x}{\sqrt{5 + x^2 + 8 \cdot x}}$$

~~$$\frac{8 + 2 \cdot x}{2 \cdot \sqrt{5 + x^2 + 8 \cdot x}} = \frac{(8 + 2 \cdot x)'}{2 \cdot (\sqrt{5 + 8 \cdot x + x^2})'} = \frac{(8)' + (2 \cdot x)'}{2 \cdot (x^2)'} = \frac{0 + 2 \cdot (x)'}{2 \cdot 2x} = \frac{2 \cdot (x)'}{4x} = \frac{2 \cdot 1}{4x} = \frac{2}{4x} = \frac{1}{2x}$$~~

$$5) \lim_{x \rightarrow +\infty} \left(\frac{n}{n-4} \right)^n = e^x \quad \times$$

$$1) z^3 = -(-i)^{886}$$

$$-1 + z^3 = 0$$

$$(-1 + z)(1 + z + z^2) = 0$$

$$z = -\frac{1}{2} + \frac{i\sqrt{3}}{2}$$

~~1) 7~~

$$z = -\sqrt[3]{-1}$$

$$-1 + z = 0 \quad 1 + z + z^2 = 0$$

$$\frac{1}{2} + z = \frac{1}{2}(-i)\sqrt{3}$$

$$z = (-1)^{\frac{2}{3}} \quad \times$$

$$\boxed{z = 1}$$

$$1 + z + z^2 = 0$$

$$z = -\frac{1}{2} + \frac{i\sqrt{3}}{2}$$

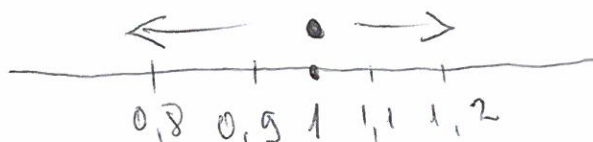
$$z + z^2 = -1$$

$$\boxed{z = -\frac{1}{2} - \frac{i\sqrt{3}}{2}} \quad \times$$

$$\frac{1}{4} z + z^2 = -\frac{3}{4}$$

$$\left(\frac{1}{2} + z\right)^2 = -\frac{3}{4}$$

$$\frac{1}{2} + z = \frac{i\sqrt{3}}{2}$$



MATEMATIKA 1: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PIŠITE DVOSTRANO!** Obavezno popuniti sva polja ispod!!

POPUNJAVA
NASTAVNIK
Broj ↓
bodova

IME I PREZIME: Luka Žilić

BROJ INDEKSA: 17-2-0208-2012

ZAOKRUŽITI AKO ŽELITE: ustmeni kod prof. Uglešića

C7

1. Među kompleksnim brojevima odrediti rješenja jednadžbe $z^3 = -(-i)^{886}$. Prikazati rješenja u kompleksnoj ravni!

10+5

2. Riješi sustav Gaussovom metodom i obavezno provjeri rješenje:

10+5

$$\begin{aligned}5x + 4z + 2t &= 3 \\x - y + 2z + t &= 1 \\4x + y + 2z &= 1 \\x + y + z + t &= 0\end{aligned}$$

3. Odrediti kada je $\frac{x+1}{\sqrt{x^2-x}} - 1 > 0$. Obavezno uvrštavanjem provjeriti rješenje jednadžbi koje se javljaju tokom rješavanja nejednadžbe.

13+2

4. Za funkciju: $f(x) = \sqrt{x^2 + 8x + 5}$ treba:

(a) pronaći drugu derivaciju

10

(b) na temelju ispitivanja toka funkcije skicirati graf

20(graf)

5. Odrediti i provjeriti rješenje $\lim_{x \rightarrow +\infty} \left(\frac{n}{n-4}\right)^n =$

8+2

6. Riješiti jednadžbu $\log_{10} x = \arctan x$ grafičkom metodom. *Provjeriti uvrštavanjem!*

10+5

Ukupno:

15

1. $z^3 = -(-i)^{886}$

$$w = \frac{x+yi}{1}$$

$$z^3 = -(-i)^2$$

$$|w| = \sqrt{x^2 + y^2} = \sqrt{1^2 + 0^2} = \sqrt{1}$$

$$z^3 = 1 \quad \checkmark$$

$$\operatorname{tg} \rho = \frac{y}{x} = \frac{0}{1} = 0$$

$$z = \sqrt[3]{1}$$

$$\rho = 0$$

$$z = \sqrt[3]{1} \cdot \left(\cos \frac{\rho + 2k\pi}{3} + i \sin \frac{\rho + 2k\pi}{3} \right) \quad k=0, 1, 2$$

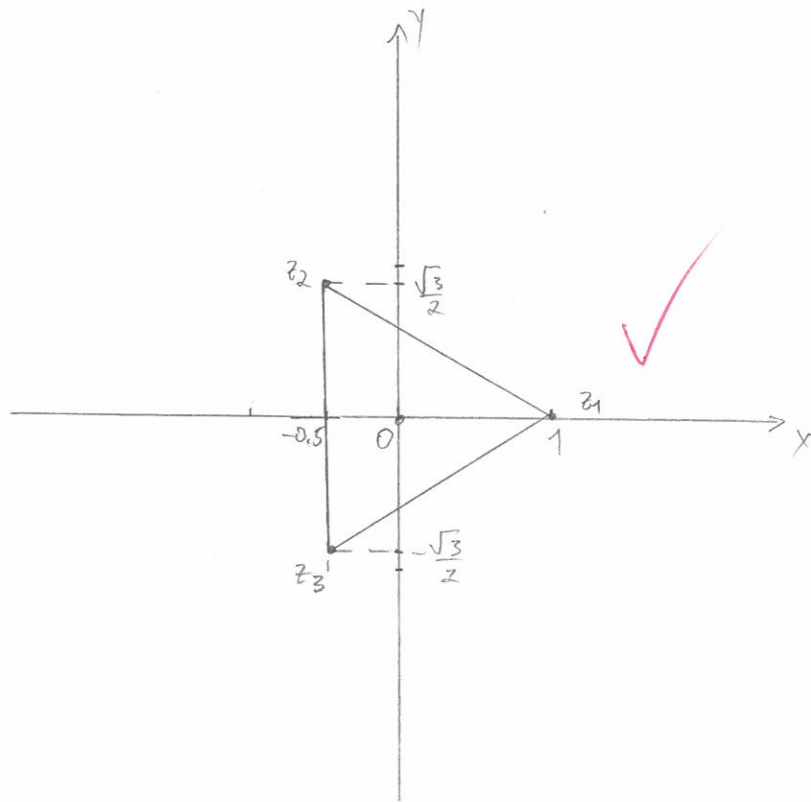
$$\begin{aligned}z_1 &= \sqrt[3]{1} \cdot \left(\cos \frac{0 + 2 \cdot 0 \cdot \pi}{3} + i \sin \frac{0 + 2 \cdot 0 \cdot \pi}{3} \right) = \\&= \sqrt[3]{1} \cdot (\cos 0 + i \sin 0) = 1 + 0i\end{aligned}$$

k=1

$$z_2 = \sqrt[3]{1} \cdot \left(\cos \frac{2}{3}\pi + i \sin \frac{2}{3}\pi \right) = -\frac{1}{2} + \frac{\sqrt{3}}{2}i$$

k=2

$$z_3 = \sqrt[3]{1} \cdot \left(\cos \frac{4}{3}\pi + i \sin \frac{4}{3}\pi \right) = -\frac{1}{2} - \frac{\sqrt{3}}{2}i$$



2.

$$5x + 4z + 2t = 3$$

$$x - y + 2z + t = 1$$

$$4x + y + 2z = 1$$

$$x + y + z + t = 0$$

$$\begin{bmatrix} 5 & 0 & 4 & 2 & | & 3 \\ 1 & -1 & 2 & 1 & | & 1 \\ 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 5 & 0 & 4 & 2 & | & 3 \\ 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix} \begin{matrix} \cdot (-5) \\ + \\ + \\ + \end{matrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 5 & -6 & -3 & | & -2 \\ 0 & 5 & -6 & -4 & | & -3 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 5 & -6 & -3 & | & -2 \\ 0 & 5 & -6 & -4 & | & -3 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 5 & -6 & -4 & | & -3 \\ 0 & 5 & -6 & -3 & | & -2 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix} \begin{matrix} \cdot (-1) \\ + \\ + \end{matrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 5 & -6 & -4 & | & -3 \\ 0 & 0 & 0 & 1 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 5 & -6 & -4 & | & -3 \\ 1 & 1 & 1 & 1 & | & 0 \\ 0 & 0 & 0 & 1 & | & 1 \end{bmatrix} \begin{matrix} \cdot (-1) \\ + \\ + \end{matrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \\ 0 & 5 & -6 & -4 & | & -3 \\ 0 & 0 & 0 & 1 & | & 1 \end{bmatrix}$$

IME I PREZIME: Luka Žilić

BROJ INDEKSA: 17-2-0208-2012

$$4. f(x) = \sqrt{x^2 + 8x + 5} = (x^2 + 8x + 5)^{\frac{1}{2}}$$

$$f'(x) = \frac{1}{2} (x^2 + 8x + 5)^{-\frac{1}{2}} \cdot (2x + 8)$$

$$f''(x) = -\frac{1}{4} (x^2 + 8x + 5)^{-\frac{3}{2}} \cdot 2x + 8 \quad \times$$

$$2. \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 1 & -1 & 2 & 1 & 1 \\ 4 & 1 & 2 & 0 & 1 \\ 5 & 0 & 4 & 2 & 3 \end{bmatrix} \begin{matrix} \cdot (-1) \\ \cdot (-4) \\ \cdot (-5) \\ \leftarrow + \\ \leftarrow + \\ \leftarrow + \end{matrix} \sim \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & -2 & 1 & 0 & 1 \\ 0 & -3 & -2 & -4 & 1 \\ 0 & -5 & -1 & -3 & 3 \end{bmatrix} \begin{matrix} \leftarrow + \\ \cdot (-1) \end{matrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & -3 & -2 & -4 & 1 \\ 0 & -5 & -1 & -3 & 3 \end{bmatrix} \cdot (-3) \sim \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & -3 & -2 & -4 & 1 \\ 0 & 15 & 3 & -9 & -9 \end{bmatrix} \begin{matrix} \cdot 5 \\ \leftarrow + \end{matrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & -3 & -2 & -4 & 1 \\ 0 & 0 & -7 & -11 & -4 \end{bmatrix} \cdot 3 \leftarrow + \sim \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 7 & 8 & 1 \\ 0 & 0 & -7 & -6 & -4 \end{bmatrix} \leftarrow +$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 7 & 8 & 1 \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \sim \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 7 & 8 & 1 \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \cdot 7 \sim \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 1 & \frac{8}{7} & \frac{1}{7} \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \cdot 2$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 1 & \frac{8}{7} & \frac{1}{7} \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \cdot \left(\frac{-8}{7}\right) \leftarrow + \sim \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 1 & 0 & \frac{17}{7} \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \cdot (-1) \leftarrow + \sim \begin{bmatrix} 1 & 0 & -2 & 0 & 0 \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 1 & 0 & \frac{17}{7} \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \cdot 2 \leftarrow +$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 & \frac{34}{7} \\ 0 & 1 & 3 & 4 & 0 \\ 0 & 0 & 1 & 0 & \frac{17}{7} \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \cdot (-3) \leftarrow + \sim \begin{bmatrix} 1 & 0 & 0 & 0 & \frac{34}{7} \\ 0 & 1 & 0 & 1 & -\frac{51}{7} \\ 0 & 0 & 1 & 0 & \frac{17}{7} \\ 0 & 0 & 0 & 2 & -4 \end{bmatrix} \cdot (-1) \leftarrow + \sim \begin{bmatrix} 1 & 0 & 0 & 0 & \frac{34}{7} \\ 0 & 1 & 0 & 0 & -\frac{37}{7} \\ 0 & 0 & 1 & 0 & \frac{17}{7} \\ 0 & 0 & 0 & 1 & -2 \end{bmatrix}$$

X

IME I PREZIME: Luka Žilić

BROJ INDEKSA: 17-2-0208-2012

b) $f(x) = \sqrt{x^2 + 8x + 5}$

DOMENA

$x^2 + 8x + 5 \geq 0$
 $a=1 \quad b=8 \quad c=5$

$x_{1,2} = \frac{-8 \pm \sqrt{64 - 20}}{2}$

$x_{1,2} = \frac{-8 \pm \sqrt{44}}{2}$

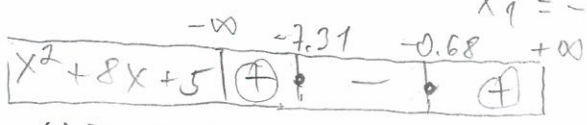
$x_1 = \frac{-8 + \sqrt{44}}{2}$

$x_2 = \frac{-8 - \sqrt{44}}{2}$



$x_1 = -0.68$

$x_2 = -7.31$



$D(f) = \langle -\infty, -7.31 \rangle \cup \langle -0.68, +\infty \rangle$

SJECISTA

$f(x) = 0$

$\text{INT}(-0.68, -7.31)$

$f(0) = x^2 + 8x + 5$
 $= 5$

$S(0, 5)$

ASIMPTOTE:

LVA:

$\lim_{x \rightarrow -7.31} \sqrt{x^2 + 8x + 5} =$

GRAF?

$$\begin{array}{l}
 2 \\
 \left[\begin{array}{cccc|c} 1 & -1 & 2 & 1 & 1 \\ 0 & 1 & -6/5 & -3/5 & -2/5 \\ 0 & 0 & 7/5 & 1/5 & -1/5 \\ 0 & 0 & 0 & -1 & -1 \end{array} \right] = \left[\begin{array}{cccc|c} 1 & -1 & 2 & 1 & 1 \\ 0 & 1 & -6/5 & -3/5 & -2/5 \\ 0 & 0 & 1 & 1/7 & -1/7 \\ 0 & 0 & 0 & -1 & -1 \end{array} \right] = \left[\begin{array}{cccc|c} 1 & -1 & 2 & 1 & 1 \\ 0 & 1 & -6/5 & -3/5 & -2/5 \\ 0 & 0 & 1 & 1/7 & -1/7 \\ 0 & 0 & 0 & 1 & 1 \end{array} \right] \approx
 \end{array}$$

$\text{III r} \cdot \frac{7}{5}$ $\text{IV r} \cdot (-1)$ $\text{IV r} \cdot (-\frac{1}{7}) + \text{III r}$
 $\text{IV r} \cdot \frac{3}{5} + \text{II r}$
 $\text{IV r} \cdot (-1) + \text{I r}$

$$\begin{array}{l}
 2 \\
 \left[\begin{array}{cccc|c} 1 & -1 & 2 & 0 & 0 \\ 0 & 1 & -6/5 & 0 & -2/5 \\ 0 & 0 & 1 & 0 & -2/7 \\ 0 & 0 & 0 & 1 & 1 \end{array} \right] = \left[\begin{array}{cccc|c} 1 & -1 & 0 & 0 & 4/7 \\ 0 & 1 & 0 & 0 & -26/35 \\ 0 & 0 & 1 & 0 & -2/7 \\ 0 & 0 & 0 & 1 & 1 \end{array} \right] = \left[\begin{array}{cccc|c} 1 & 0 & 0 & 0 & -6/35 \\ 0 & 1 & 0 & 0 & -26/35 \\ 0 & 0 & 1 & 0 & -2/7 \\ 0 & 0 & 0 & 1 & 1 \end{array} \right]
 \end{array}$$

$\text{III r} \cdot 6/5 + \text{II r}$ $\text{II r} \cdot 1 + \text{I r}$
 $\text{III r} \cdot (-2) + \text{I r}$

a) $5 \cdot (-\frac{6}{35}) + 0 \cdot (-\frac{26}{35}) + 4 \cdot (-\frac{2}{7}) + 2 \cdot 1 = 3$
 $-\frac{6}{7} + 0 - \frac{8}{7} + 2 = 3$
 $0 \neq 3 \quad \leftarrow$

PROVJERA:

b) $-\frac{6}{35} - (-\frac{26}{35}) + 2 \cdot (-\frac{2}{7}) + 1 = 1$
 $1 = 1$

c) $4 \cdot (-\frac{6}{35}) - \frac{26}{35} + 2 \cdot (-\frac{2}{7}) + 1 = 1$
 $-1 \neq 1$

d) $-\frac{6}{35} - \frac{26}{35} - \frac{2}{7} + 1 = 1$
 $-\frac{1}{5} \neq 0$

$$\begin{array}{l}
 5x + 4z + 2t = 3 \\
 x - y + 2z + t = 1 \\
 4x + y + 2z = 1 \\
 x + y + z + t = 0
 \end{array}$$

MATEMATIKA 1: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PIŠITE DVOSTRANO!** Obavezno popuniti sva polja ispod!!

POPUNJAVA
NASTAVNIK
Broj ↓
bodova

IME I PREZIME: *Petra Ugrinić*

BROJ INDEKSA: *17-1-0123-2012*

ZAOKRUŽITI AKO ŽELITE: ustmeni kod prof. Uglešića

C7

1. Među kompleksnim brojevima odrediti rješenja jednadžbe $z^3 = -(-i)^{886}$. Prikazati rješenja u kompleksnoj ravni!

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10+5

Ukupno:

2.

$$\left[\begin{array}{cccc|c} 5 & 0 & 4 & 2 & 3 \\ 1 & -1 & 2 & 1 & 1 \\ 4 & 1 & 2 & 0 & 1 \\ 1 & 1 & 1 & 1 & 0 \end{array} \right] \begin{array}{l} \text{I} - \text{II} \\ \text{III} - \text{IV} \end{array} \sim \left[\begin{array}{cccc|c} 4 & 1 & 2 & 1 & 2 \\ 1 & -1 & 2 & 1 & 1 \\ 3 & 0 & 1 & -1 & 1 \\ 1 & 1 & 1 & 1 & 0 \end{array} \right] \begin{array}{l} \text{I} - \text{II} \\ \sim \end{array} \left[\begin{array}{cccc|c} 3 & 0 & 0 & 0 & 1 \\ 1 & -1 & 2 & 1 & 1 \\ 3 & 0 & 1 & -1 & 1 \\ 1 & 1 & 1 & 1 & 0 \end{array} \right] \begin{array}{l} /:2, \\ \end{array}$$

?

6. $\underbrace{\log_{10} x}_x = \underbrace{\arctan x}_y$

| x | log ₁₀ |
|---|-------------------|
| 0 | 0.0 |
| 1 | 0 |
| 2 | 0.3 |
| 4 | 0.6 |

| x | arctan |
|------|--------|
| 0 | 0 |
| 0.01 | 0.57 |
| 0.02 | 1.14 |
| 0.03 | 1.71 |