

odgovornosti studenata. **PIŠITE DVOSTRANO!**

IME I PREZIME: **LUKA LOKAČIĆ**

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Želim ustmeni kod (zaokružiti):

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asistent Kosor

1. Riješiti diferencijalnu jednačbu: $y'' - y' = e^x + 1$. 15

2. Odrediti lokalne ekstreme funkcije $f(x, y) = x^3 - 3xy - y^3$. 15

3. Pronaći ravninu koja dira graf funkcije $f(x, y) = y\sqrt{x} - y^2 - x + 6y$ povučenu u točki $(4, 1, z_0)$ tog grafa. 15

4. Numeričkom integracijom procijeniti vrijednost $\int_0^1 \frac{dx}{1 + \sqrt{x}}$, a zatim isti integral riješiti egzaktno Newton

Leibnitzovom formulom.

10+5

5. $\int_2^3 \frac{2x^2 + x + 2}{x^2 - 1} dx =$

20

6. $\int_0^2 \frac{x - 1}{x^2 + x - 2} dx = ?$

20

Ukupno:

10

f	$\frac{df}{dx}$
$x^\alpha (\alpha \neq 0)$	$\alpha x^{\alpha-1}$
$\ln x$	$\frac{1}{x}$
$\log_\alpha x (\alpha > 0)$	$\frac{1}{x \ln \alpha}$
e^x	e^x
$\alpha^x (\alpha > 0)$	$\alpha^x \ln \alpha$
$\sin x$	$\cos x$
$\cos x$	$-\sin x$
$\tan x$	$\frac{1}{\cos^2 x}$
$\cot x$	$\frac{-1}{\sin^2 x}$
$\arcsin x$	$\frac{1}{\sqrt{1-x^2}}$
$\arctan x$	$\frac{1}{1+x^2}$

Tablica nekih integrala		
$\int dx = x + C$	$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \arctan \frac{x}{a} + C$	$\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left \frac{a+x}{a-x} \right + C$
$\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1}, \alpha \neq -1$	$\int \tan x dx = -\ln \cos x + C$	$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left \frac{x-a}{x+a} \right + C$
$\int \frac{dx}{x} = \ln x + C$	$\int \cot x dx = \ln \sin x + C$	$\int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln \left x + \sqrt{x^2 \pm a^2} \right + C$
$\int e^x dx = e^x + C$	$\int \frac{dx}{\cos^2 x} = \tan x + C$	$\int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + C$
$\int a^x dx = \frac{a^x}{\ln a} + C$	$\int \frac{dx}{\sin^2 x} = -\cot x + C$	$\int \frac{dx}{\sqrt{2ax - x^2}} = \arccos \left(1 - \frac{x}{a} \right) + C$
$\int \sin x dx = -\cos x + C$	$\int \sqrt{x^2 \pm a^2} dx = \frac{1}{2} \left[x\sqrt{x^2 \pm a^2} \pm a^2 \ln \left(x + \sqrt{x^2 \pm a^2} \right) \right] + C$	
$\int \cos x dx = \sin x + C$	$\int \sqrt{a^2 - x^2} dx = \frac{1}{2} \left[x\sqrt{a^2 - x^2} + a^2 \arcsin \left(\frac{x}{a} \right) \right] + C$	

$$\textcircled{4} \int_0^1 \frac{dx}{1+\sqrt{x}} \Rightarrow y = \frac{1}{1+\sqrt{x}}$$

$$S = \frac{1}{6} (1 + 4 \cdot 0,5858 + 0,5)$$

$$S = 0,640 \quad \checkmark$$

x	0	1	2
x_a	0	1/2	1
$f(x)$	1	0,5858	0,5

$$d = 1 - 0 = 1$$

$$\textcircled{1} \begin{aligned} y'' - y' &= e^x + 1 \\ \lambda^2 - \lambda &= e^x + 1 \end{aligned}$$

$$y = c \cdot e^{2x}$$

✗

$$\textcircled{5} \int_2^3 \frac{2x^2 + x + 2}{x^2 - 1} dx$$

$$= \int_2^3 \frac{2x^2}{x^2 - 1} dx + \int_2^3 \frac{x dx}{x^2 - 1} + \int_2^3 \frac{2 dx}{x^2 - 1}$$

$$= 2 \int_2^3 \frac{x^2}{x^2 - 1} dx + \int_2^3 \frac{x}{x^2 - 1} dx + 2 \int_2^3 \frac{dx}{x^2 - 1}$$

$$= \frac{1}{2} \left| \frac{1}{2} |x^2 + 1| \right|_2^3 + 2 \left| \frac{1}{2} \ln \left| \frac{x-1}{x+1} \right| \right|_2^3$$

