

MATEMATIKA 2: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PIŠITE DVOSTRANO!**

POPUNJAVA
NASTAVNIK
Broj ↓
bodova
ixx

IME I PREZIME: ELENA BEG

BROJ INDEKSA: 17-2-0181-2012

1. Pronaći opće rješenje ODJ $4y'' - 4y' = 2x + 3$ i provjeriti dobiveno rješenje. 15
2. Odrediti lokalne ekstreme funkcije $f(x, y) = \sin x + \cos y$. 15 8
3. Pronaći ravninu koja dira graf funkcije $f(x, y) = y\sqrt{x} - y^2 - x + 6y$ povučenu u točki $(4, 1, z_0)$ tog grafa. 15
4. $\int_0^2 2x^2 \cos x \, dx = ?$ 20
5. $\int_0^1 \frac{2x}{x^2 - 4} \, dx = ?$ 15
6. Izračunati površinu područja omeđenog krivuljama $y^2 - 2y - 2 + x = 0$ i $x + y + 1 = 0$. 20

Ukupno:

43

f	$\frac{df}{dx}$
$x^\alpha (\alpha \neq 0)$	$\alpha x^{\alpha-1}$
$\ln x$	$\frac{1}{x}$
$\log_\alpha x (\alpha > 0)$	$\frac{1}{x \ln \alpha}$
e^x	e^x
$\alpha^x (\alpha > 0)$	$\alpha^x \ln \alpha$
$\sin x$	$\cos x$
$\cos x$	$-\sin x$
$\tan x$	$\frac{1}{\cos^2 x}$
$\cot x$	$\frac{-1}{\sin^2 x}$
$\arcsin x$	$\frac{1}{\sqrt{1-x^2}}$
$\arctan x$	$\frac{1}{1+x^2}$

Tablica nekih integrala		
$\int dx = x + C$	$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \arctan \frac{x}{a} + C$	$\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left \frac{a+x}{a-x} \right + C$
$\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1}, \alpha \neq -1$	$\int \tan x dx = -\ln \cos x + C$	$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left \frac{x-a}{x+a} \right + C$
$\int \frac{dx}{x} = \ln x + C$	$\int \cot x dx = \ln \sin x + C$	$\int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln \left x + \sqrt{x^2 \pm a^2} \right + C$
$\int e^x dx = e^x + C$	$\int \frac{dx}{\cos^2 x} = \tan x + C$	$\int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + C$
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$\int \cos x dx = \sin x + C$	$\int \sqrt{a^2 - x^2} dx = \frac{1}{2} \left[x\sqrt{a^2 - x^2} + a^2 \arcsin \left(\frac{x}{a} \right) \right] + C$	

$$C_1 e^{rx} + C_2 e^{-rx}$$

$$(1) \quad 4y'' - 4y' = 2x + 3$$

$$4r^2 - 4r = 0$$

$$r_{1,2} = \frac{4 \pm \sqrt{16-4 \cdot 0 \cdot 4}}{2 \cdot 4}$$

$$r_{1,2} = \frac{4 \pm 4}{8} \quad r_1 = 1 \quad r_2 = 0$$

$$g(x) = 2x + 3$$

$$\begin{aligned} g(x) &= e^{rx} (P_m(x) \cos(\beta x) + Q_m(x) \sin(\beta x)) \\ &= e^{0 \cdot x} ((2x+3) \cos(0 \cdot x) + 0 \cdot \sin(0 \cdot x)) \\ &\quad \omega = 0 \quad m = 1 \quad \beta = 0 \quad n = 0 \end{aligned}$$

$$N = 1$$

$$\omega + \beta \omega = 0 \quad k = 1$$

$$y_p = x^k e^{rx} (S_N(x) \cos(\beta x) + T_N(x) \sin(\beta x))$$

$$y_p = x^1 e^{0 \cdot x} ((Ax+B) \cos(0 \cdot x) + (Cx+D) \sin(0 \cdot x))$$

$$y_p = x(Ax+B)$$

$$y_p = Ax^2 + Bx$$

$$y'_p = 2Ax + B$$

$$y'_p = 2A$$

$$4 \cdot (2A) - 4(2Ax + B) = 2x + 3$$

$$8A - 8Ax - 4B = 2x + 3$$

$$\text{Uz } x: \quad -8A = 2 \quad /:(-8)$$

$$A = -\frac{1}{4}$$

$$\text{dann: } 8A - 4B = 3$$

$$8 \cdot \left(-\frac{1}{4}\right) - 4B = 3$$

$$-2 - 4B = 3$$

$$-4B = 3 + 2$$

$$-4B = 5 \quad /:(-4)$$

$$B = -\frac{5}{4}$$

$$y_p = Ax^2 + Bx$$

$$y_p = -\frac{1}{4}x^2 - \frac{5}{4}x$$

$$y = y_H + y_p$$

$$y = C_1 x + C_2 - \frac{1}{4}x^2 - \frac{5}{4}x$$

$$\textcircled{2} \quad f(x,y) = \sin x + \cos y$$

$$\frac{\partial f}{\partial x} = \cos x$$

$$\frac{\partial f}{\partial y} = -\sin y$$

$$\cos x = 0$$

$$x = \frac{\pi}{2} + k\pi, z \in \mathbb{Z}$$

$$-\sin y = 0$$

$$y = 0 + k\pi$$

$$\frac{\partial^2 f}{\partial x^2} = -\sin x = A$$

$$\frac{\partial^2 f}{\partial y^2} = -\cos y = C$$

$$\frac{\partial^2 f}{\partial xy} = 0 = B$$

$T(\frac{\pi}{2}, 0) \rightarrow \text{STACIONARNA TOČKA}$

PROUSTILI STE
LOKALNI MINIMUM
 $\checkmark T(\frac{3\pi}{2}, \pi)$

$$\Delta = AC - B^2 = (-\sin(\frac{\pi}{2})) \cdot (-\cos 0) - 0$$

$$= -1 \cdot (-1) - 0 = 1 \quad \Delta > 0$$

$$A = -1 < 0$$

8

$$f(\frac{\pi}{2}, 0) = \sin(\frac{\pi}{2}) + \cos 0 =$$

$T(\frac{\pi}{2}, 0) \rightarrow \text{LOKALNI MAXIMUM}$

$$= 1 + 1 = 2$$

točka u kojoj maximum postize svoju vrednost.

$$T(\frac{\pi}{2}, 0, 2)$$

$$\textcircled{3} \quad f(x,y) = \sqrt{x-y^2} - x + 6y$$

$$T(4, 1, z_0) \rightarrow 1 \cdot \sqrt{4} - 1 - 4 + 6 \cdot 1 = z_0$$

$$T(4, 1, 3)$$

$$\frac{\partial f}{\partial x} = \frac{1}{2\sqrt{x}} - 1$$

$$fx(t) = \frac{1}{2\sqrt{4}} - 1 = -\frac{3}{4}$$

$$3 = z_0$$

$$Rt... z - z_0 = fx(t)(x - x_0) + fy(t)(y - y_0)$$

$$Rt... z - 3 = -\frac{3}{4}(x - 4) + 6(y - 1)$$

$$\frac{\partial f}{\partial y} = \sqrt{x-y^2} + 6$$

$$fy(t) = \sqrt{4} - 2 \cdot 1 + 6$$

$$= 2 - 2 + 6$$

$$= 6$$

$$Rt... z - 3 = -\frac{3}{4}x + 3 + 6y - 6$$

$$z - 3 = -\frac{3}{4}x + 6y - 3$$

$$z = -\frac{3}{4}x + 6y - 3 + 3$$

$$z = -\frac{3}{4}x + 6y$$

15

(4.) $\int_0^2 2x^2 \cos x \, dx =$ $D_f = \mathbb{R}$
17-2-0181-2012

$$\left[\begin{array}{l} u = 2x^2 \\ du = 4x \, dx \end{array} \quad \begin{array}{l} dv = \cos x \, dx \\ v = \int \cos x \, dx \\ v = \sin x + C \end{array} \right] = 2x^2 \sin x - \int 4x \sin x \, dx =$$

$$\left[\begin{array}{l} u = 4x \\ du = 4 \, dx \end{array} \quad \begin{array}{l} dv = \sin x \, dx \\ v = -\cos x + C \end{array} \right] =$$

$$= 2x^2 \sin x + 4x \cos x + \int 4 \cos x \, dx =$$

$$= 2x^2 \sin x + 4x \cos x - 4 \int \cos x \, dx =$$

$$= 2x^2 \sin x + 4x \cos x - 4 \sin x + C \Big|_0^2$$

$$= 2 \cdot 4 \sin 2 + 4 \cdot 2 \cos 2 - 4 \cdot \sin 0 - (4 \cdot 0 \sin 0 + 4 \cdot 0 \cos 0 - 4 \cdot \sin 0)$$

$$= 0,3080150149 - 0 = \boxed{0,3080150149} \quad \checkmark \underline{20}$$

(5.) $\int_0^1 \frac{2x}{x^2-4} \, dx$ $x^2-4 \neq 0$
 $x^2 \neq 4$
 $x \neq \pm 2$ \checkmark

$$\int_0^1 \frac{2x}{x^2-4} \, dx = \left[\begin{array}{l} t = x^2 - 4 \\ dt = 2x \, dx \end{array} \quad \begin{array}{l} 2ax = 1 \rightarrow t = 1-4 \\ t = -3 \\ 2ax = 0 \rightarrow t = 0-4 \\ t = -4 \end{array} \right]$$

$$\int_{-4}^{-3} \frac{dt}{t} = [\ln|t|]_{-4}^{-3} = \left[\ln|x^2-4| \right]_{-4}^{-3} =$$

$$= \ln 5 - \ln 12 = \boxed{-0,8754687374} \quad \times$$

$$⑥ \quad y^2 - 2y - 2 + x = 0$$

$$y^2 - 2y - 2 = -x$$

$$y - x = y^2 - 2y - 2 \quad | : (-1)$$

$$x = -y^2 + 2y + 2$$

\downarrow
ZAMJENA VARIJABLJ

$$y = -x^2 + 2x + 2$$

$$x + y + 1 = 0$$

$$y = -x - 1$$

$$-x - 1 = 0$$

$$-x = 1$$

$$x = -1$$

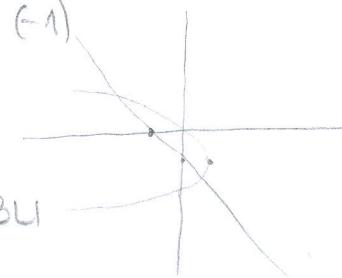
$$(-1, 0)$$

$$y = x^2 + x + c$$

$$-0 - 1 = y$$

$$-1 = y$$

$$(0, -1)$$



$$\cancel{-x^2 + 2x - 2 = -x - 1}$$

$$\cancel{-x^2 + 2x + x - 2 + 1 = 0}$$

$$\cancel{-x^2 + 3x - 1 = 0}$$

$$x_{1,2} = \frac{-3 \pm \sqrt{9 - 4 \cdot (-1) \cdot (-1)}}{-2}$$

$$x_1 = \frac{-3 + \sqrt{5}}{-2} = \frac{3 - \sqrt{5}}{2} \approx 0,3819$$

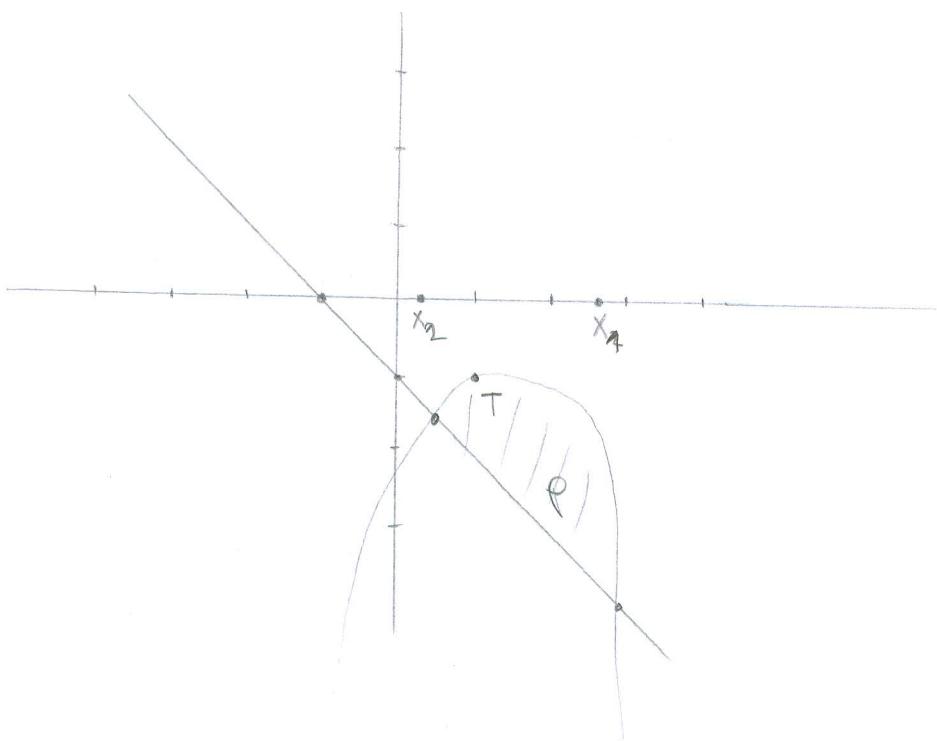
$$x_2 = \frac{-3 - \sqrt{5}}{-2} = \frac{3 + \sqrt{5}}{2} \approx 2,618$$

SJECISTA

$$x_0 = -\frac{b}{2a} = -\frac{2}{2 \cdot (-1)} = 1$$

$$y_0 = -1 + 2 \cdot 1 - 2 = -1$$

$T(1, -1) \rightarrow$ tjeremo parabolic



$$\underline{x^2 + 2x - 2 = -x - 1} \quad X$$

$$-x^2 + 2x + x - 2 + 1 = 0$$

$$-x^2 + 3x - 1 = 0 \quad | \cdot (-1)$$

$$x^2 - 3x + 1 = 0$$

$$x_{1,2} = \frac{3 \pm \sqrt{9-4 \cdot 1 \cdot 1}}{2} =$$

$$x_1 = \frac{3+\sqrt{5}}{2} = 2,61 \quad x_2 = \frac{3-\sqrt{5}}{2} = 0,38 \quad \rightarrow \text{JUECISTA}$$

$$P = \int_{\frac{3-\sqrt{5}}{2}}^{\frac{3+\sqrt{5}}{2}} (-x^2 + 2x - 2 + x + 1) dx = \int_{\frac{3-\sqrt{5}}{2}}^{\frac{3+\sqrt{5}}{2}} (-x^2 + 3x - 1) dx =$$

$$= \left[-\frac{x^3}{3} + \frac{3x^2}{2} - x \right]_{\frac{3-\sqrt{5}}{2}}^{\frac{3+\sqrt{5}}{2}} =$$

$$= \left(-\frac{\left(\frac{3+\sqrt{5}}{2}\right)^3}{3} + \frac{3 \cdot \left(\frac{3+\sqrt{5}}{2}\right)^2}{2} - \left(\frac{3+\sqrt{5}}{2}\right) \right)$$

$$= -\frac{9-4\sqrt{5}}{3} + \frac{21+9\sqrt{5}}{4} - \left(\frac{3+\sqrt{5}}{2}\right) = \boxed{\frac{9+5\sqrt{5}}{12}}$$

$$2 - \frac{\left(\frac{3-\sqrt{5}}{2}\right)^3}{3} + \frac{3 \cdot \left(\frac{3-\sqrt{5}}{2}\right)^2}{2} - \left(\frac{3-\sqrt{5}}{2}\right) =$$

$$= -\frac{9+4\sqrt{5}}{3} + \frac{21-9\sqrt{5}}{4} - \left(\frac{3-\sqrt{5}}{2}\right) = -\frac{9+5\sqrt{5}}{12}$$

$$P = \frac{9+5\sqrt{5}}{12} + \left(-\frac{9+5\sqrt{5}}{12}\right)$$

$$\boxed{P = \frac{5\sqrt{5}}{6}}$$

MATEMATIKA 2: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PISITE DVOSTRANO!**

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IME I PREZIME: **BRANIMIR PIJACIĆ**

BROJ INDEKSA:

17-2-0086-2011

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Ukupno: **0**

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$$(6) \int_0^2 2x^2 \cos x dx = \left[\begin{array}{l} u = 2x^2 \\ du = 4x dx \\ v = \int \cos x dx \\ v = \sin x \end{array} \right] \quad \begin{array}{l} du = \cos x \\ v = \int \cos x dx \end{array}$$

$$2x^2 \cdot \sin x - \int_0^2 \sin x \cdot 4x dx = \left[\begin{array}{l} u = 4x \\ du = 4 \\ v = \int \sin x dx \end{array} \right] \quad \begin{array}{l} u = 4x \\ du = 4 \\ v = -\cos x \end{array}$$

$$2x^2 \cdot \sin x - \left[4x \cdot -\cos x - \int_0^2 4x \cdot -\cos x \right]$$

$$2x^2 \cdot \sin x + 4x \cdot \cos x + 4 \int_0^2 \sin x dx$$

$$2 \cdot 2^2 \cdot \sin(2) + 4 \cdot 2 \cdot \cos(2) + 4 \int_0^2 \sin x dx - \left[2 \cdot 0^2 + \sin(0) + 4 \cdot 0 \cdot \cos(0) + 4 \sin(0) \right]$$

$$= 8.41 - 0 \approx 8.41 \quad // \quad \text{O}$$

$$\textcircled{5} \quad \int_0^1 \frac{2x}{x^2 - 4} = \left| \begin{array}{l} x^2 - 4 = t \\ 2x dx = dt \end{array} \right.$$

$$\int_{-4}^{-3} \frac{dt}{t} =$$

$$\cancel{\int_{-4}^{-3} \ln(t) dt} = \ln|x^2 - 4|$$

$$= \ln|(-3)^2 - 4| - \ln|(-4)^2 - 4| \quad \cancel{\phi}$$

$$= \ln|5| - \ln|12|$$

-1.0

$$\textcircled{6} \quad y^2 - 2y - 2 + x = 0$$

$$x + y + 1 = 0$$

$$y^2 - 2y - 2 - y - 1 = 0$$

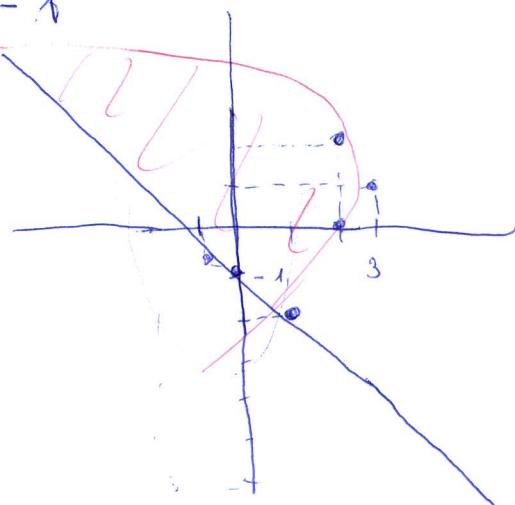
$$x = -y - 1$$

$$y^2 - 3y - 3 = 0$$

$$x_{1,2} = \frac{3 \pm \sqrt{9+12}}{2}$$

$$x_1 = 3,75 \quad x_2 = -0,75$$

$$\int_{-0,75}^{3,75}$$



$$P = 0,$$

Krivulje međusobno ne zatvaraju očekenu površinu

$$\begin{array}{c|ccccc} x & 3 & 2 & 2 & -1 & -5 \\ \hline y & 1 & 0 & 2 & -1 & -2 \end{array}$$

$$\begin{array}{c|ccccc} x & -1 & 0 & 1 \\ \hline y & 0 & -1 & -2 \end{array}$$

Branimir

Pijac

17-2-0086-2011

2) $f(x,y) = \sin x + \cos y$

$$f_x = \cos x \quad f_{xy} = -\sin y$$

$$f_{xx} = -\sin x \quad f_{yy} = -\cos y$$

$$f_{xy} = 0$$

$$f_{xx} = 0$$

$$\begin{aligned} & \left(\cos \frac{\pi}{2} = 0 \right) \\ & \cos x \neq 0 \quad -\sin y = 0 \\ & x \neq \cancel{\frac{\pi}{2}} \quad y = 0 \end{aligned}$$

nema ekstrema \times

$$\cos x \neq 0$$

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IME I PREZIME: Nemanja Korda

BROJ INDEKSA:

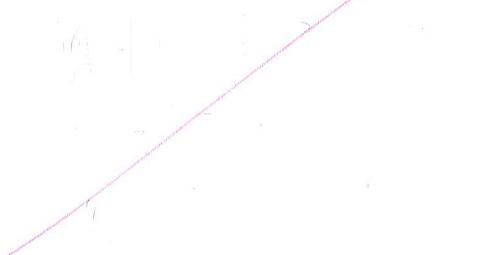
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$\int \sin x dx = -\cos x + C$	$\int \sqrt{x^2 \pm a^2} dx = \frac{1}{2} \left[x \sqrt{x^2 \pm a^2} \pm a^2 \ln \left(x + \sqrt{x^2 \pm a^2} \right) \right] + C$	
$\int \cos x dx = \sin x + C$	$\int \sqrt{a^2 - x^2} dx = \frac{1}{2} \left[x \sqrt{a^2 - x^2} + a^2 \arcsin \left(\frac{x}{a} \right) \right] + C$	

Ukupno:

Q1 $4y'' - 4y' = 2x + 3$



$$\textcircled{4} \quad \int_0^2 2x^2 \cos x dx$$

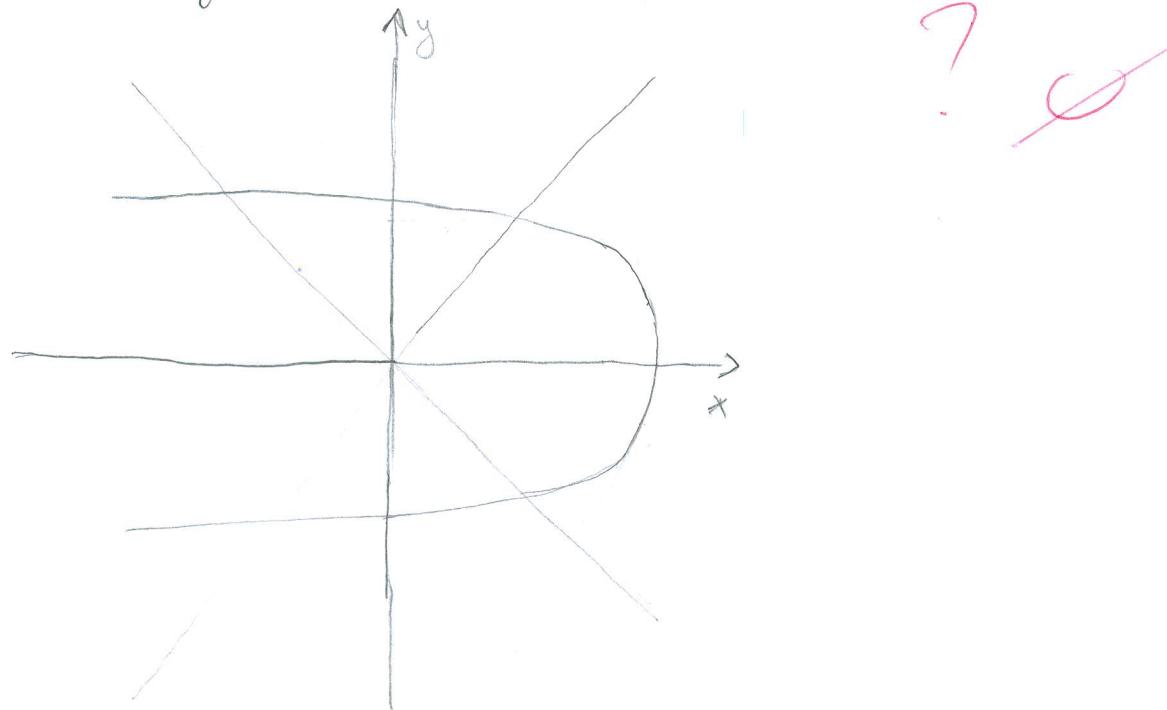
$$\int_0^2 2 \cdot 2x^{2-1} \cdot (-\sin x) \cdot dx \quad ?$$

$$\int_0^2 4x - \sin x dx$$

$$-4 \int_0^2 x - \sin x dx$$

~~$$-4 \int_0^2 x \sin x dx$$~~

$$\textcircled{6} \quad y^2 - 2y - 2 + x = 0 \quad x + y + 1 = 0$$



MATEMATIKA 2: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **Pišite dvostrano!**

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POPUNJAVA
NASTAVNIK
Broj ↓
bodova

IME I PREZIME:

Šimun Ždrilic

BROJ INDEKSA:

02 6980562

1. Pronaći opće rješenje ODJ $4y'' - 4y' = 2x + 3$ i provjeriti dobiveno rješenje. 15
 2. Odrediti lokalne ekstreme funkcije $f(x, y) = \sin x + \cos y$. 15
 3. Pronaći ravnicu koja dira graf funkcije $f(x, y) = y\sqrt{x} - y^2 - x + 6y$ povučenu u točki $(4, 1, z_0)$ tog grafa. 15
 4. $\int_0^2 2x^2 \cos x \, dx = ?$ 20
 5. $\int_0^1 \frac{2x}{x^2 - 4} = ?$ 15
 6. Izračunati površinu područja omeđenog krivuljama $y^2 - 2y - 2 + x = 0$ i $x + y + 1 = 0$. 20
-

f	$\frac{df}{dx}$
$x^\alpha (\alpha \neq 0)$	$\alpha x^{\alpha-1}$
$\ln x$	$\frac{1}{x}$
$\log_\alpha x (\alpha > 0)$	$\frac{1}{x \ln \alpha}$
e^x	e^x
$\alpha^x (\alpha > 0)$	$\alpha^x \ln \alpha$
$\sin x$	$\cos x$
$\cos x$	$-\sin x$
$\tan x$	$\frac{1}{\cos^2 x}$
$\cot x$	$\frac{-1}{\sin^2 x}$
$\arcsin x$	$\frac{1}{\sqrt{1-x^2}}$
$\arctan x$	$\frac{1}{1+x^2}$

Tablica nekih integrala		
$\int dx = x + C$	$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \arctan \frac{x}{a} + C$	$\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left \frac{a+x}{a-x} \right + C$
$\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1}, \alpha \neq -1$	$\int \tan x dx = -\ln \cos x + C$	$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left \frac{x-a}{x+a} \right + C$
$\int \frac{dx}{x} = \ln x + C$	$\int \cot x dx = \ln \sin x + C$	$\int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln x + \sqrt{x^2 \pm a^2} + C$
$\int e^x dx = e^x + C$	$\int \frac{dx}{\cos^2 x} = \tan x + C$	$\int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + C$
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Ukupno:

0

MATEMATIKA 2: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **Pišite dvostrano!**

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POPUNJAVA
NASTAVNIK
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bodova

IME I PREZIME: GABRIJELA JORDAN

BROJ INDEKSA:

17-2-0118-20M

1. Pronaći opće rješenje ODJ $4y'' - 4y' = 2x + 3$ i provjeriti dobiveno rješenje. 15
 2. Odrediti lokalne ekstreme funkcije $f(x, y) = \sin x + \cos y$. 15
 3. Pronaći ravninu koja dira graf funkcije $f(x, y) = y\sqrt{x} - y^2 - x + 6y$ povučenu u točki $(4, 1, z_0)$ tog grafa. 15
 4. $\int_0^2 2x^2 \cos x \, dx = ?$ 20
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 6. Izračunati površinu područja omeđenog krivuljama $y^2 - 2y - 2 + x = 0$ i $x + y + 1 = 0$. 20
-

Ukupno:

f	$\frac{df}{dx}$
$x^\alpha (\alpha \neq 0)$	$\alpha x^{\alpha-1}$
$\ln x$	$\frac{1}{x}$
$\log_\alpha x (\alpha > 0)$	$\frac{1}{x \ln \alpha}$
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IZBACENA ZBOG "IGRANJA" MOBITELOM

4. $\int_0^2 2x^2 \cos x \, dx$

5. $\int_0^1 \frac{2x}{x^2 - 4} \, dx$

$$y^2 - 2y - 2 + x = 0 \quad | \quad x + y + 1 = 0$$

$$y^2 - 2y - 2 + x = 0 \quad | \quad x + y + 1 = 0$$

$$y^2 - 2y - 2 + x = 0$$

MATEMATIKA 2: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **Pišite dvostrano!**

IME I PREZIME: DAVOR SERTIC

BROJ INDEKSA: 0269055501

17-2-0092-2011

POPUNJAVA
NASTAVNIK
Broj ↓
bodova

1. Pronaći opće rješenje ODJ $4y'' - 4y' = 2x + 3$ i provjeriti dobiveno rješenje. 15
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Ukupno:

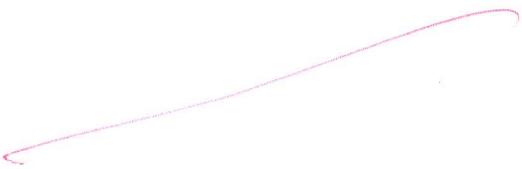
f	$\frac{df}{dx}$
$x^\alpha (\alpha \neq 0)$	$\alpha x^{\alpha-1}$
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$\log_\alpha x (\alpha > 0)$	$\frac{1}{x \ln \alpha}$
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① Pronaći opće rješenje ODJ $4y'' - 4y' = 2x + 3$ i provjeriti dobiveno rješenje.

② Odrediti lokalne ekstreme funkcije $f(x, y) = \sin x + \cos y$

③ Problém máme když máme funkcií $f(x,y) = y\sqrt{x} - y^2 - x + 6y$
 počítat u toku (y_1, z_0) tohoto grafu



$$\textcircled{4} \quad \int_0^2 2x^2 \cos x \, dx = ?$$

$$\textcircled{5} \quad \int_0^1 \frac{2x}{x^2 - 4} \, dx = ?$$

⑥ Izracuji povrch podle podmínek daných kruvými rovnicemi $y^2 - 2y - 2 + x = 0$

$$1 \quad x + y + 1 = 0$$

MATEMATIKA 2: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **Pišite dvostrano!**

IME I PREZIME: LUKA GULAN

BROJ INDEKSA: 0242017933

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POPUNJAVA
NASTAVNIK
Broj ↓
bodova

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