

MATEMATIKA 1: Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata. **PIŠITE DVOSTRANO!** Obavezno popuniti sva polja ispod!!

POPUNJAVA
NASTAVNIK
Broj ↓
bodova

C7

IME I PREZIME: **TONI STOŠIĆ**

BROJ INDEKSA:

ZAKRUŽITI AKO ŽELITE: ustmeni kod prof. Uglešića

1. Među kompleksnim brojevima odrediti rješenja jednadžbe $z^3 = -(-i)^{843}$. Prikazati rješenja u kompleksnoj ravnini!

10+5

2. Riješi sustav Gaussovom metodom i obavezno provjeri rješenje:

10+5

$$\begin{aligned} 5x + 4z + 2t &= 3 \\ x - y + 2z + t &= 1 \\ 4x + y + 2z &= 1 \\ x + y + z + t &= 0 \end{aligned}$$

3. Odrediti kada je $\frac{x+1}{\sqrt{x^2-x}} - 1 > 0$. Obavezno uvrštavanjem provjeriti rješenje jednadžbi koje se javljaju tokom rješavanja nejednadžbe.

13+2

4. Za funkciju: $f(x) = \sqrt{x^2 + 4x + 5}$ treba:

(a) pronaći drugu derivaciju

10

(b) na temelju ispitivanja toka funkcije skicirati graf

20(graf)

5. Odrediti i provjeriti rješenje $\lim_{x \rightarrow +\infty} \left(\frac{n}{n-4}\right)^n =$

8+2

6. Riješiti jednadžbu $\log_{10} x = \arctan x$ grafičkom metodom. *Provjeriti uvrštavanjem!*

10+5

Ukupno:

10

1.

$$\begin{aligned} z^3 &= -(-i)^{843} \\ z^3 &= i^{843} \\ z^3 &= -i \\ z &= \sqrt[3]{-i} \end{aligned}$$

$$843 : 4 = 210$$

$$4 \cdot 210 = 840$$

$$840 : 3 = 280$$

$$280 : 3 = 93 \text{ ostatak } 1$$

$$93 : 3 = 31$$

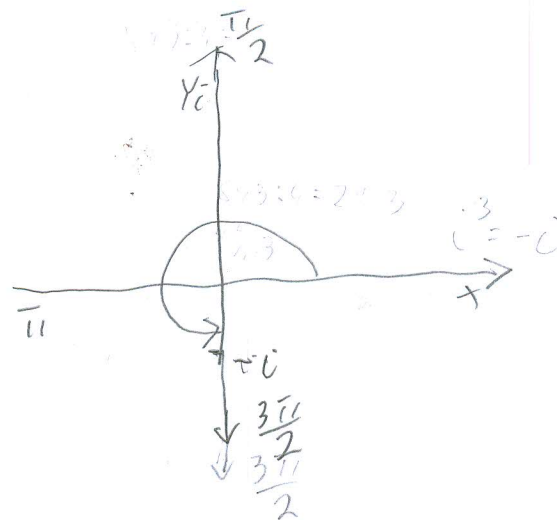
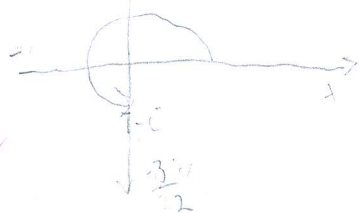
$$31 : 3 = 10 \text{ ostatak } 1$$

$$10 : 3 = 3 \text{ ostatak } 1$$

$$3 : 3 = 1$$

$$1 : 3 = 0 \text{ ostatak } 1$$

$$z^3 = i^{280+3+1+1+1} = i^{286} = i^{285+1} = (i^3)^{95} \cdot i = -i$$



$$z_k, k=0,1,2$$

$$\varphi = \frac{3\pi}{2}$$

$$a) z_k = \sqrt[3]{1} \left(\cos \frac{\varphi + k \cdot 2\pi}{n} + i \sin \frac{\varphi + k \cdot 2\pi}{n} \right)$$

$$z_0 = \sqrt[3]{1} \left(\cos \frac{3\pi/2 + 0 \cdot 2\pi}{3} + i \sin \frac{3\pi/2 + 0 \cdot 2\pi}{3} \right)$$

$$z_0 = 1 \left(\cos 157 + i \sin 157 \right)$$

$$z_0 = 0.007 + i 0.989$$

$$z_2 = ?$$

$$z_3 = ?$$

$$|w| = \sqrt{x^2 + y^2}$$

$$|w| = \sqrt{0^2 + 1^2}$$

$$|w| = \sqrt{1} = 1$$

2.

$$\begin{bmatrix} 5 & 0 & 4 & 2 & | & 3 \\ 1 & -1 & 2 & 1 & | & 1 \\ 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 5 & 0 & 4 & 2 & | & 3 \\ 4 & 1 & 2 & 0 & | & 1 \\ 1 & 1 & 1 & 1 & | & 0 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 5 & -6 & -3 & | & -2 \\ 0 & 5 & -6 & -4 & | & -3 \\ 0 & 0 & -1 & 0 & | & -1 \end{bmatrix}$$

$1R \leftrightarrow 2R$
 $1R \cdot (-5) + 2R$
 $1R \cdot (-4) + 3R$
 $1R \cdot (-1) + 4R$
 $2R = 5$

$$\begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 1 & -6/5 & 3/5 & | & -2/5 \\ 0 & 5 & -6 & -4 & | & -3 \\ 0 & 0 & -1 & 0 & | & -1 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 1 & -6/5 & 3/5 & | & -2/5 \\ 0 & 0 & 0 & -1 & | & -1 \\ 0 & 0 & -1 & 0 & | & -1 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 1 & -6/5 & 3/5 & | & -2/5 \\ 0 & 0 & -1 & 0 & | & -1 \\ 0 & 0 & 0 & -1 & | & -1 \end{bmatrix}$$

$2R \cdot (-5) + 3R$
 $3 \leftrightarrow 4$
 $3R \cdot (-1)$
 $4R \cdot (-1)$

$$\begin{bmatrix} 1 & -1 & 2 & 1 & | & 1 \\ 0 & 1 & -6/5 & 3/5 & | & -2/5 \\ 0 & 0 & 1 & 0 & | & 1 \\ 0 & 0 & 0 & 1 & | & 1 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 2 & 0 & | & 0 \\ 0 & 1 & -6/5 & 0 & | & 1/5 \\ 0 & 0 & 1 & 0 & | & 1 \\ 0 & 0 & 0 & 1 & | & 1 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & 0 & 0 & | & -2 \\ 0 & 1 & 0 & 0 & | & 7/5 \\ 0 & 0 & 1 & 0 & | & 1 \\ 0 & 0 & 0 & 1 & | & 1 \end{bmatrix} \sim \begin{bmatrix} 1 & 0 & 0 & 0 & | & 3/5 \\ 0 & 1 & 0 & 0 & | & 7/5 \\ 0 & 0 & 1 & 0 & | & 1 \\ 0 & 0 & 0 & 1 & | & 1 \end{bmatrix}$$

$4R \cdot (-3/5) + 2R$
 $4R \cdot (-1) + 1R$
 $3R \cdot (-6/5) + 2R$
 $3R \cdot (-2) + 1R$
 $2R \cdot 1 + 1R$
 $1/5 \cdot 1 = 1/5$

proyena:

a) $5 \cdot (-\frac{3}{5}) + 0 \cdot \frac{4}{5} + 4 \cdot 1 + 2 \cdot 1 = 3$

$-\frac{15}{5} + 0 + 4 + 2 = 3$
 $-\frac{15}{5} + 0 + 3 = 3$

b) $1 \cdot (-\frac{3}{5}) - 1 \cdot \frac{4}{5} + 2 \cdot 1 + 1 \cdot 1 = 1$

$-\frac{3}{5} - \frac{4}{5} + 2 + 1 = 1$
 $-\frac{10}{5} + 2 + 1 = 1$
 $1 = 1$

c) $4 \cdot (-\frac{3}{5}) + 1 \cdot \frac{4}{5} + 2 \cdot 1 + 0 \cdot 1 = 1$

$-\frac{12}{5} + \frac{4}{5} + 2 + 0 = 1$
 $-\frac{5}{5} + 2 + 0 = 1$
 $1 = 1$

d) $1 \cdot (-\frac{3}{5}) + 1 \cdot \frac{4}{5} + 1 \cdot 1 + 1 \cdot 1 = 0$

$-\frac{3}{5} + \frac{4}{5} + 1 + 1 = 0$
 $\frac{-3+4+5+5}{5} = 0$
 $0 = 0$

$x = -\frac{3}{5}$
 $y = \frac{4}{5}$
 $z = 1$
 $t = 1$

TOMI STOSIC

4. NASTAVA 4

DOMENA:

$$x^2 + 4x + 5 \neq 0$$

$$\Delta = 1, 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x_1 = \frac{-4 + \sqrt{4^2 - 4 \cdot 1 \cdot 5}}{2}$$

$$x_2 = \frac{-4 + \sqrt{-4}}{2}$$

$$x_1 = \frac{-4 + 2}{2} = -1$$

$$x_2 = \frac{-4 - 2}{2} = -3$$

3. Derivacija

\Rightarrow PRE SVOJENA

PARNOST:

$$f(x) = f(-x)$$

$$\sqrt{x^2 + 4x + 5} = \sqrt{x^2 - 4x + 5}$$

NIJE PARNA
NIJE PERIODICNA

$$\begin{array}{cccc} -\infty & -3 & -1 & +\infty \\ | & + & - & + & | \end{array}$$

$$D(f) = (-\infty, -3] \cup [-1, +\infty)$$

ASIMTOIC:

V.A NEMA jer tocke nisu u domeni

H.A.

$$\lim_{x \rightarrow +\infty} \sqrt{x^2 + 4x + 2} = \lim_{x \rightarrow +\infty} \frac{x^2}{x^2} + \frac{x}{x^2} + \frac{2}{x^2} = 1$$

1 = D.H. 4

$$\lim_{x \rightarrow -\infty} \sqrt{x^2 + 4x + 2} \left[\begin{array}{l} x \rightarrow -x \\ -\infty \rightarrow +\infty \end{array} \right] =$$

$$\lim_{x \rightarrow -\infty} \sqrt{x^2 - 4x + 2} = \lim_{x \rightarrow +\infty} \frac{x^2}{x^2} - \frac{4}{x} + \frac{2}{x^2} = 1$$

L.H.A

K.A NEMA jer im H.A

GRAFI?

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