

Popunite odmah!

IME I PREZIME: **MARKO BANIBIĆ**

Broj indeksa: **54952-2007**

40

DATUM: 21.2.2012. VRIJEME: OD

DO

MATEMATIKA 1: Trajanje 120 minuta. Ispit se održava sukladno objavljenim pravilima. Na snazi je Pravilnik o stegovnoj odgovornosti studenata.

7
Broj ↓
bodova
20

1. Odrediti točke infleksije funkcije $f(x) = \ln(x^2 + 1)$.

2. Odrediti i ispitati sve asimptote funkcije $g(x) = \frac{x}{\ln x}$.

3. Riješiti među kompleksnim brojevima $\frac{z-i}{z^2-i} = 2$. Možete koristiti formulu za multočke kvadratne funkcije. 20

4. Odrediti sva koja postoje riješenja sustava linearnih jednadžbi i provjeriti:

~~15+5~~

$$\begin{aligned} x_1 - x_2 + x_3 &= 4 \\ 2x_1 + 2x_2 + 6x_3 &= 6 \\ -x_1 - 2x_2 - 4x_3 &= -4 \\ -4x_1 - x_2 - 9x_3 &= -16 \end{aligned}$$

5. Ispitati period (ako postoji) i ograničenost funkcije $h(x) = \sin(4x)$

5+15

$$\begin{array}{l} 4. \quad x_1 - x_2 + x_3 = 4 \\ \quad 2x_1 + 2x_2 + 6x_3 = 6 \\ \quad -x_1 - 2x_2 - 4x_3 = -4 \\ \quad -4x_1 - x_2 - 9x_3 = -16 \end{array} \quad \left| \begin{array}{ccc|c} 1 & -1 & 1 & 4 \\ 2 & 2 & 6 & 6 \\ -1 & -2 & -4 & -4 \\ -4 & -1 & -9 & -16 \end{array} \right. \begin{array}{l} R_2 - 2R_1 \\ R_3 + R_1 \\ R_4 + 4R_1 \end{array} \sim \left| \begin{array}{ccc|c} 1 & -1 & 1 & 4 \\ 0 & 4 & 4 & -2 \\ 0 & -3 & -3 & 0 \\ 0 & -5 & -8 & 0 \end{array} \right. \begin{array}{l} R_2 : 4 \\ \sim \end{array} \left| \begin{array}{ccc|c} 1 & -1 & 1 & 4 \\ 0 & 1 & 1 & -\frac{1}{2} \\ 0 & -3 & -3 & 0 \\ 0 & -5 & -8 & 0 \end{array} \right. \begin{array}{l} R_1 + R_2 \\ \sim \\ R_3 + 3R_2 \\ R_4 + 5R_2 \end{array}$$

$$\left| \begin{array}{ccc|c} 1 & 0 & \frac{3}{2} & \frac{7}{2} \\ 0 & 1 & \frac{3}{2} & -\frac{1}{2} \\ 0 & 0 & \frac{3}{2} & -\frac{3}{2} \\ 0 & 0 & -\frac{1}{2} & -\frac{5}{2} \end{array} \right. \begin{array}{l} R_3 : (-\frac{3}{2}) \\ \sim \end{array} \left| \begin{array}{ccc|c} 1 & 0 & \frac{3}{2} & \frac{7}{2} \\ 0 & 1 & \frac{3}{2} & -\frac{1}{2} \\ 0 & 0 & 1 & 2 \\ 0 & 0 & -\frac{1}{2} & -\frac{5}{2} \end{array} \right. \begin{array}{l} R_1 - \frac{3}{2}R_3 \\ R_2 - \frac{3}{2}R_3 \\ \sim \\ R_4 + \frac{1}{2}R_3 \end{array} \left| \begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -\frac{5}{2} \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 6 \end{array} \right. \begin{array}{l} R_4 : 6 \\ \sim \end{array} \left| \begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -2 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{array} \right. \begin{array}{l} R_4 : 6 \\ \sim \end{array} \left| \begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -2 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{array} \right. \begin{array}{l} R_1 + 2R_2 \\ R_3 - 2R_4 \end{array}$$

NEMA RJEŠENJA

$$\left[\begin{array}{ccc|c} 1 & -1 & 1 & 4 \\ 2 & 2 & 6 & 6 \\ -1 & -2 & -4 & -4 \\ -4 & -1 & -9 & -16 \end{array} \right] \begin{array}{l} \left(\begin{array}{c} 0 \\ -2 \\ 2 \\ 1 \end{array} \right) \\ = \left(\begin{array}{c} 4 \\ 6 \\ -4 \\ -16 \end{array} \right) \end{array} \quad \times$$

$$\begin{aligned} \frac{7}{2} - \left(2 \cdot \frac{4}{4}\right) &= \frac{7}{2} - \frac{14}{4} = \frac{14}{4} - \frac{14}{4} = 0 \\ -\frac{1}{2} - \left(2 \cdot \frac{3}{4}\right) &= -\frac{1}{2} - \frac{6}{4} = \frac{-2}{4} - \frac{6}{4} = \frac{-8}{4} = -2 \\ -\frac{5}{2} + \left(2 \cdot \frac{17}{4}\right) &= -\frac{5}{2} + \frac{34}{4} = \frac{-10}{4} + \frac{34}{4} = \frac{24}{4} = 6 \\ -3 + \left(3 \cdot \frac{3}{4}\right) &= -3 + \frac{9}{4} = \frac{-12}{4} + \frac{9}{4} = \frac{-3}{4} \end{aligned}$$

1. $f(x) = \ln(x^2+1)$

KRITICKE TOČKE

$$f'(x) = \ln(x^2+1)' = \frac{1}{(x^2+1)} \cdot 2x = \frac{2x}{(x^2+1)} = 0$$

$$2x = 0 \quad x = 0$$

NOŽNI UVJET ZA INFLEKSIJU:

$$f''(x) = \left(\frac{2x}{(x^2+1)} \right)' = \frac{2 \cdot (x^2+1) - 2x \cdot 2x}{(x^2+1)^2} = \frac{2x^2+2-4x^2}{(x^2+1)^2} = \frac{-2x^2+2}{(x^2+1)^2} = 0$$

$$-2x^2+2=0$$

$$a=-2 \quad b=0 \quad c=2$$

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4 \cdot a \cdot c}}{2 \cdot a} = \frac{0 \pm \sqrt{0^2 - 4 \cdot (-2) \cdot 2}}{2 \cdot (-2)}$$

$$x_{1,2} = \frac{0 \pm 4}{-4}$$

$$x_1 = -1 \quad \underline{\underline{(-1, 0)}} \rightarrow \text{INFLEKSIJA}$$

$$x_2 = 1 \quad \underline{\underline{(1, 0)}} \rightarrow \text{INFLEKSIJA}$$

	$-\infty$	-2	-1	0	1	2	$+\infty$
$f''(x)$		-	+	-			
$f'(x)$		e	e	e			



