

Popunite odmah!

IME I PREZIME: Toma Medic

BROJ INDEKSA: 17-2-0052

62

DATUM: 28.09.2019 VRIJEME: OD 13:35 DO

MATEMATIKA 1: Trajanje 100 minuta. Zabranjen je razgovor sa drugim studentima. ZADATKE RIJEŠAVATE JEDNOSTRANO NA PAPIRE KOJE DOBIJETE OD NASTAVNIKA.

xoxo
Broj ↓
bodova

1. Odrediti determinantu matrice $A = \begin{bmatrix} 1 & 2 & 0 & 0 & 0 \\ 1 & 1 & 2 & 0 & 0 \\ 0 & 1 & 1 & 2 & 0 \\ 0 & 0 & 1 & 1 & 2 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix}$

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2. Odrediti domenu i sve asimptote funkcije $f(x) = x + \sqrt{x^2 + x + 1}$

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3. Ispitati konvergenciju reda $\sum \left(\frac{n^2 + 4n + 4}{2n + 2n^2} \right)^{2n}$

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4. Ispitati domenu, periodičnost, parnost i prvu derivaciju funkcije $g(x) = \ln(\sin(3x))$.

7

5. Na temelju ispitivanja toka funkcije napraviti skicu grafa funkcije $h(x) = \frac{x^2 + 2}{x^2 + 1}$.

15

3) $\sum_{n=1}^{\infty} \left(\frac{n^2 + 4n + 4}{2n + 2n^2} \right)^{2n}$ CAUCHY $L = \lim_{n \rightarrow \infty} \sqrt[n]{a_n}$

$L = \lim_{n \rightarrow \infty} \sqrt[n]{\left(\frac{n^2 + 4n + 4}{2n + 2n^2} \right)^{2n}} = \lim_{n \rightarrow \infty} \frac{(n^2 + 4n + 4)^2 \cdot \frac{1}{n^2}}{(2n + 2n^2)^2 \cdot \frac{1}{n^2}} = \lim_{n \rightarrow \infty} \frac{\left(1 + \frac{4}{n} + \frac{4}{n^2}\right)^2}{\left(\frac{2}{n} + 2\right)^2} = \frac{(1)^2}{(2)^2} = \frac{1}{4}$

$L < 1$ RED KONVERGIRA ✓ 20
 $\frac{1}{4} < 1$

h.) $y(x) = \ln(\sin(3x))$

3° DERIVACIJA
 $f'(x) = \frac{1}{\sin(3x)} \cdot \cos(3x) \cdot 3$ ✓

1° DOMENA $D(f) = (0, \infty)$
 $\sin(3x) > 0$
 $3x > 0$
 $x > 0$ ✗

$f''(x) = \frac{\cos(3x)}{\sin^2(3x)} \cdot (-)$
 $f''(x) = -3 \cot(3x)$ 7

2° PARNOST

$g(x) = \ln(\sin(3x))$
 $g(-x) = \ln(\sin(-3x))$ ✗
 $g(-x) = -\ln(\sin(3x))$

3° PERIODIČNOST
NIJE PERIODIČNA

$f(x) = -f(x)$
NEPARNA

VIDI ŽIKIĆ

$$2.) f(x) = x + \sqrt{x^2 + x + 1}$$

$$x^2 + x + 1 \geq 0$$

$$\mathcal{D}(f) = \mathbb{R}$$

VIDI ŠIKIĆ

$$x_{1,2} = \frac{-1 \pm \sqrt{1-4}}{2}$$

$$x_{1,1} = \frac{-1 \pm \sqrt{3}}{2}$$

Nije zadovoljen uvjet Doračun

$$1.) \begin{bmatrix} 1 & 2 & 0 & 0 & 0 \\ 1 & 1 & 2 & 0 & 0 \\ 0 & 1 & 1 & 2 & 0 \\ 0 & 0 & 1 & 1 & 2 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix} = 1 \begin{bmatrix} 1 & 2 & 0 & 0 \\ 1 & 1 & 2 & 0 \\ 0 & 1 & 1 & 2 \\ 0 & 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1 & 2 & 0 & 0 \\ 0 & 1 & 1 & 2 \\ 0 & 0 & 1 & 1 \end{bmatrix} =$$

$$= 1 \left[1 \begin{bmatrix} 1 & 2 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1 & 2 & 0 \\ 0 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} \right] - 2 \left[1 \begin{bmatrix} 1 & 2 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} \right] =$$

$$= 1 \left[1 \begin{bmatrix} 1-2 & & \\ 1 & 1-2 & \\ 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1-0 & & \\ 1 & 2 & \\ 0 & 1 & \end{bmatrix} \right] - 2 \left[1 \begin{bmatrix} 1-2 & & \\ 1 & 1-2 & \\ 0 & 1 & 1 \end{bmatrix} \right] - 2 \left[1 \begin{bmatrix} 1-2 & & \\ 1 & 1-2 & \\ 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1-0 & & \\ 1 & 2 & \\ 0 & 1 & \end{bmatrix} \right] =$$

$$= 1 \left[1 \begin{bmatrix} -1 & & -2 \\ 1 & -1 & \\ 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1 & & \\ 1 & 1 & \\ 0 & 1 & \end{bmatrix} \right] - 2 \left[1 \begin{bmatrix} -1 & & \\ 1 & -1 & \\ 0 & 1 & 1 \end{bmatrix} \right] - 2 \left[1 \begin{bmatrix} 1 & & \\ 1 & -1 & \\ 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1 & & \\ 1 & 1 & \\ 0 & 1 & \end{bmatrix} \right] =$$

$$= 1 \left[1 \begin{bmatrix} -3 & & \\ 1 & & \\ 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} -1 & & \\ 1 & & \\ 0 & 1 & 1 \end{bmatrix} \right] - 2 \left[1 \begin{bmatrix} -3 & & \\ 1 & & \\ 0 & 1 & 1 \end{bmatrix} \right] =$$

$$= 1 \left[1 \begin{bmatrix} -3 & +2 \\ 1 & & \\ 0 & 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} -3 & & \\ 1 & & \\ 0 & 1 & 1 \end{bmatrix} \right] = -1 + 6 = 5$$

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3) $h(x) = \frac{x^2+2}{x^2+1}$

$D(f) = \mathbb{R}$

1° DOMENA

2° PARNOST

$h(x) = \frac{x^2+2}{x^2+1}$

$h(-x) = \frac{(-x)^2+2}{(-x)^2+1} = \frac{x^2+2}{x^2+1}$

$f(x) = f(-x)$
PARNA

3° PERIODIČNOST

NJE PERIODIČNA

4° NULTOČKE

NEMA NULTOČKI

$f(x) = 0$

$x^2+2=0$

$x^2 = -2$

$x = \sqrt{-2}$

$x = i\sqrt{2}$

5° ASIMPTOTE

a) VERTIKALNIH ASIMPTOTA NEMA JER JE DODANA FUNKCIJE \mathbb{R}

b) HORIZONTALNE ASIMPTOTE

$\lim_{x \rightarrow \infty} \frac{x^2+2}{x^2+1} = \lim_{x \rightarrow \infty} \frac{1 + \frac{2}{x^2}}{1 + \frac{1}{x^2}} = \frac{1}{1} = 1$

$\frac{1}{1} = 1$

$\lim_{x \rightarrow -\infty} \frac{x^2+2}{x^2+1} = [x \rightarrow -x] = \lim_{x \rightarrow \infty} \frac{(-x)^2+2}{(-x)^2+1} = \lim_{x \rightarrow \infty} \frac{x^2+2}{x^2+1} = \lim_{x \rightarrow \infty} \frac{1 + \frac{2}{x^2}}{1 + \frac{1}{x^2}} = \frac{1}{1} = 1$

c) KOSIH ASIMPTOTA NEMA JER IMAMO HORIZONTALNU

6° EKSTREMI

$$f'(x) = \frac{2x(x^2+1) - 2x(x^3+2)}{(x^2+1)^2} = \frac{2x^3+2x-2x^4-4x}{(x^2+1)^2} = \frac{-2x}{(x^2+1)^2}$$

$-2x = 0$

$x = 0$

POTENCIJALI
EKSTREM

$$f''(x) = \frac{-2(x^2+1) - 2(x^3+1) \cdot 2x \cdot (-2x)}{(x^2+1)^4} \quad \times$$

$$f''(x) = \frac{-2(x^2+1) + 8x^2(x^2+1)}{(x^2+1)^4} \quad \times$$

$$f''(x) = \frac{(x^2+1)(-2+8x^2)}{(x^2+1)^4}$$

$$f''(x) = \frac{-2+8x^2}{(x^2+1)^3}$$

$$f''(0) = \frac{-2+0}{(0+1)^3} = -2$$

7° INTERVALI MONOTONOSTI

x	$-\infty$	0	∞
f'(x)	+		-
f(x)	\nearrow		\searrow

L. max

$$f(0) = \frac{2}{(1+1)^2} = \frac{2}{4} = \frac{1}{2}$$

$$f(0) = \frac{0+2}{0+1} = 2$$

M(0, 2)

$$f(1) = \frac{-2}{(1+1)^2} = -\frac{1}{2}$$

$f''(x)$ IMA POZITIVAN
NAZIVNIK

PREDZNAK $f''(x)$ OVISI O
BROJNIKU

GDJE JE $-2+8x^2 \geq 0$?

GDJE JE $-2+8x^2 = 0$

$\Rightarrow x = \pm \frac{1}{2}$

$\Rightarrow f''(x)$

	$-\infty$	$-\frac{1}{2}$	$\frac{1}{2}$	$+\infty$
f''(x)	+	+	+	
f(x)	\nearrow	\searrow	\searrow	

8° INTERVALI LAKRIVJENOSTI

x	$-\infty$	0	$+\infty$
f''(x)	-	+	
f(x)	\cap	\cap	

$$f''(1) = \frac{-2+8}{(1+1)^3} = \frac{6}{8} = \frac{3}{4}$$

$$f''(-1) = \frac{-2+8}{(1+1)^3} = \frac{6}{8} = \frac{3}{4}$$

$f''(x) = 0$

$-2+8x^2 = 0$

$8x^2 = 2$

$x^2 = \frac{1}{4}$

$x = \pm \frac{1}{2}$

NEMA TOČAKA

LAKRIVJENOSTI

IME I PREZIME:

Toma Molić

BROJ INDEKSA: 17-2-0032

5° 64+

$$h(x) = \frac{x^2 + 2}{x^2 + 1}$$

$$h(1) = \frac{1+2}{1+1} = \frac{3}{2}$$

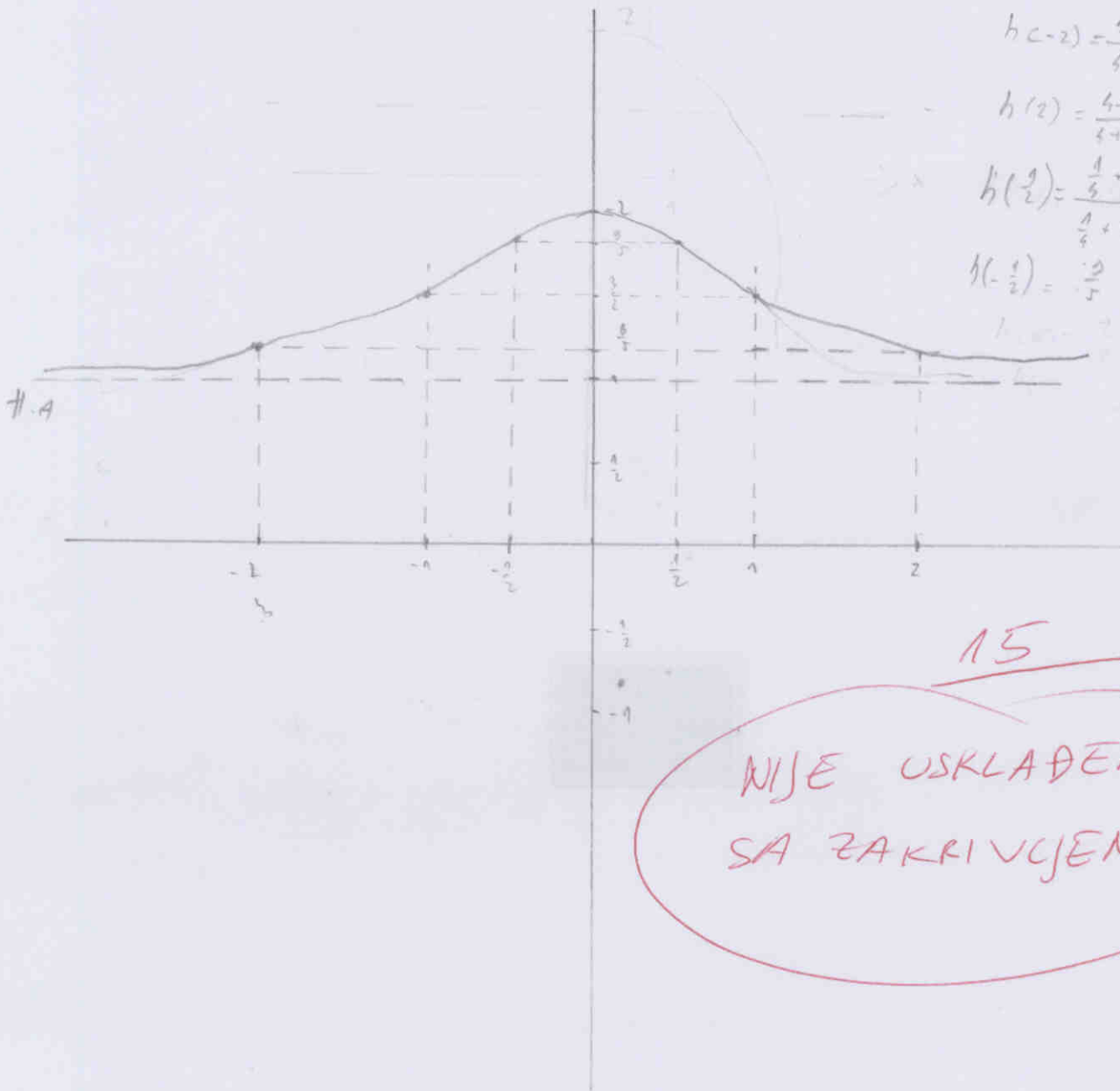
$$h(-1) = \frac{1+2}{1+1} = \frac{3}{2}$$

$$h(-2) = \frac{4+2}{4+1} = \frac{6}{5}$$

$$h(2) = \frac{4+2}{4+1} = \frac{6}{5}$$

$$h\left(\frac{1}{2}\right) = \frac{\frac{1}{4} + 2}{\frac{1}{4} + 1} = \frac{\frac{9}{4}}{\frac{5}{4}} = \frac{9}{5}$$

$$h\left(-\frac{1}{2}\right) = \frac{9}{5}$$



15

NIJE USKLAĐENO
SA ZAKRIVLJENOSTI

28.4.2010.

IME I PREZIME:

IVAN ŠIKIĆ

BROJ INDEKSA:

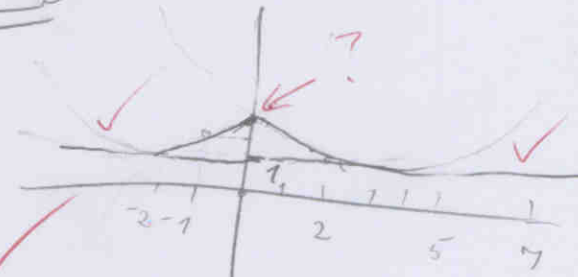
17-1-0014-2010

$$5. f(x) = \frac{x^2+2}{x^2+1}, \quad Df = \mathbb{R} \quad \underline{\underline{x^2+1 > 0}}$$

f -ija nije periodična, ne sadrži

traj. x -ije nije neparna, parna je. ✓

Postupa funkciji, nema polova, nema V.A.



$$\lim_{x \rightarrow 0} \frac{x^2+2}{x^2+1} = \frac{2}{1} = 2$$

$$\text{D.H.A.} \quad \lim_{x \rightarrow +\infty} \frac{x^2+2}{x^2+1} = \frac{\infty}{\infty} = \frac{x^2+2 \text{ } | : x^2}{x^2+1 \text{ } | : x^2} = \frac{1}{1} = 1 \quad \checkmark$$

$$\text{L.H.A.} \quad \lim_{x \rightarrow -\infty} \frac{(-x)^2+2}{(-x)^2+1} = \frac{\infty}{\infty} = 1 \quad \checkmark$$

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$$f'(x) = \frac{(x^2+1)' \cdot (x^2+2) - (x^2+1)' \cdot (x^2+2)}{(x^2+1)^2} = \frac{2x \cdot (x^2+2) - 2x \cdot (x^2+1)}{(x^2+1)^2}$$

VIDI

$$= \frac{2x^3+4x-2x^3-2x}{(x^2+1)^2} = \frac{2x}{(x^2+1)^2} = \frac{2x}{x^4+2x^2+1}$$

$$f''(x) = \frac{(x^4+2x^2+1)' \cdot 2x - (x^4+2x^2+1)' \cdot 2}{(x^2+1)^4} = \frac{(4x^3+4x) \cdot 2x - 2x^4 - 4x^2 - 2}{(x^2+1)^4}$$

$$= \frac{8x^4+8x^2-2x^4-4x^2-2}{(x^2+1)^4} = \frac{6x^4+4x^2-2}{(x^2+1)^4}$$

28.4.2011.

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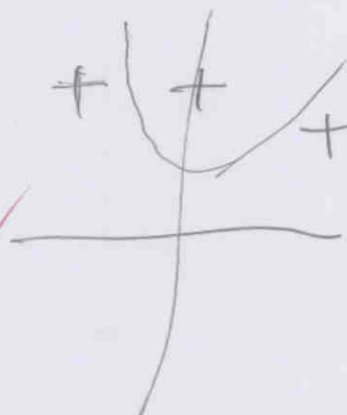
BROJ INDEKSA:

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$$2. f(x) = x + \sqrt{x^2 + x + 1}$$

D.H.A.

$$D(f) = \mathbb{R} \checkmark$$



$$\lim_{x \rightarrow \infty} x + \sqrt{x^2 + x + 1} = \lim_{x \rightarrow \infty} x + \sqrt{x^2 + x + 1} \cdot \frac{x - \sqrt{x^2 + x + 1}}{x - \sqrt{x^2 + x + 1}} =$$

$$\lim_{x \rightarrow \infty} \frac{x^2 - x^2 - x - 1}{x - \sqrt{x^2 + x + 1}} = \lim_{x \rightarrow \infty} \frac{-x - 1}{x - \sqrt{x^2 + x + 1}} \cdot \frac{1}{x} =$$

$$\lim_{x \rightarrow \infty} \frac{-1 + \frac{1}{x}}{1 - \sqrt{1 + \frac{1}{x} + \frac{1}{x^2}}} = \frac{-1}{1 - 1} = \frac{-1}{0} \text{ NEMA D.H.A, MOŽDA IMA}$$

DESNU KOSU. \checkmark

28.4.2011.

IME I PREZIME:
MASTAVAK,

IVAN ŠIKIĆ

BROJ INDEKSA:

17-1-0014-2010

2. L.H.A.

$$\lim_{x \rightarrow -\infty} -x + \sqrt{(-x)^2 + x + 1} = \lim_{x \rightarrow -\infty} -x + \sqrt{x^2 - x + 1} \cdot \frac{-x + \sqrt{x^2 - x + 1}}{-x - \sqrt{x^2 - x + 1}}$$

$$= \lim_{x \rightarrow -\infty} \frac{x^2 - x^2 + x + 1}{-x - \sqrt{x^2 - x + 1}} = \lim_{x \rightarrow -\infty} \frac{x - 1}{-x - \sqrt{x^2 - x + 1}} = \lim_{x \rightarrow -\infty} \frac{-1 + \frac{1}{x}}{-1 - \sqrt{1 - \frac{1}{x} + \frac{1}{x^2}}}$$

$$= \lim_{x \rightarrow -\infty} \frac{-1}{-2} = \frac{-1}{2} \text{ je L.H.A. } \checkmark$$

D.K.A.

$$\lim_{x \rightarrow \infty} \left(\frac{f(x)}{x} \right) \Rightarrow \lim_{x \rightarrow \infty} \frac{x + \sqrt{x^2 + x + 1}}{x} \Rightarrow \lim_{x \rightarrow \infty} \left(1 + \frac{\sqrt{x^2 + x + 1}}{x} \right)$$

$$= 1 + \lim_{x \rightarrow \infty} \frac{\sqrt{x^2 + x + 1}}{x} = 1 + \lim_{x \rightarrow \infty} \frac{x^2 + x + 1}{x^2} =$$

$$= 1 + \lim_{x \rightarrow \infty} \frac{1}{1} = 2$$

$k=2 \checkmark$
 $y = kx + e$

$$\lim_{x \rightarrow \infty} (f(x) + kx) = \lim_{x \rightarrow \infty} (x + \sqrt{x^2 + x + 1} - 2x) =$$

$$\lim_{x \rightarrow \infty} (-x + \sqrt{x^2 + x + 1}) = \lim_{x \rightarrow \infty} -x + \sqrt{x^2 + x + 1} \cdot \frac{-x - \sqrt{x^2 + x + 1}}{-x - \sqrt{x^2 + x + 1}}$$

$$= \lim_{x \rightarrow \infty} \frac{x^2 - \sqrt{x^2 + x + 1} - x - 1}{-x - \sqrt{x^2 + x + 1}} = \lim_{x \rightarrow \infty} \frac{-x - 1}{-x - \sqrt{x^2 + x + 1}} = \lim_{x \rightarrow \infty} \frac{-1 - \frac{1}{x}}{-1 - 1}$$

$$= \lim_{x \rightarrow \infty} \frac{-1}{-2} = \frac{1}{2}$$

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$y = 2x + \frac{1}{2} \Rightarrow$ DOKA ASIMPT. \checkmark

28.4.2011.

IME I PREZIME: NAN ŠIKIĆ

BROJ INDEKSA: 17-1-0014-2010

2. V.A.

$$x^2 + 4x + 1 = 0$$

$$x_{1,2} = \frac{-1 \pm \sqrt{1-4}}{2}$$

$$x_{1,2} = \frac{-1 \pm \sqrt{-3}}{2}$$

što nije nema rešenja n.T., nema V.A. ✓

3.

$$\sum \left(\frac{n^2 + 4n + 4}{2n + 2n^2} \right)^{2n} = \left(1 + \frac{1}{n}\right)^m$$

$$\lim_{n \rightarrow \infty} \frac{(n+2)^2}{(n+1)2n}$$

$$n^2 + 4n + 4 \Rightarrow (n+2)^2$$

$$2n + 2n^2 \Rightarrow (n+1)2n$$

$$\frac{(n+2)^2}{(n+1)2n} = \frac{n^2 + 4n + 4}{n^2 + 2n + 1}$$



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28.4. 2011.

IME I PREZIME: IVAN ŠIKIĆ

BROJ INDEKSA:

17-1-0014-2010

4. $g(x) = \ln(\sin 3x)$



$$\sin 3x > 0 \quad \Bigg| \quad \sin \frac{3\pi}{2} > 0$$

$\sin x \Rightarrow$ NEPARNA F-ija?

$$D_f(\sin x) = \mathbb{R}, \quad \text{Pr} = \left[-\frac{\pi}{2} + 2k\pi, \frac{\pi}{2} + 2k\pi\right]$$

$$D_f(\ln x) = \langle 0, +\infty \rangle$$

$$D_f(\ln(\sin 3x)) = \left[-\frac{3\pi}{2} + 3k\pi, +\infty\right)$$

Funkcija je periodična,
sadrži trig. f-ija u sebi.

NIJE PARNIA, NI TI NEPARNA
PERIOD?

$$g(x) = \ln(\sin(3x))$$

$$f(x) = \sin 3x$$

$$f'(x) = \cos 3x \cdot 3$$

$$(\ln x)' = \frac{1}{x}$$

7

$$g'(x) = \frac{f'(x)}{f(x)} = \frac{\cos 3x \cdot 3}{\sin 3x} = \frac{3 \cos 3x}{\sin 3x} = 3 \cot 3x$$

NEPARNOST: DA LI JE $f(x) = -f(-x)$

$$\text{ILI } -f(x) = f(-x)$$

$$\text{NPR ZA } x=1: -f(1) = f(-1)?$$

PERIOD: $\sin x = \sin(x + 2\pi)$
 $\sin 3x = \sin(3x + 2\pi) = \sin\left(3\left(x + \frac{2\pi}{3}\right)\right)$
 $\Rightarrow f(x) = f\left(x + \frac{2\pi}{3}\right) \Rightarrow P = \frac{2\pi}{3}$

IME I PREZIME:

IVAN ŠIKIĆ

BROJ INDEKSA:

28.9.2010.

17.1-0014-2010

Popuniti odmah!

IME I PREZIME: Mateja Kocić

BRJ INDEKSA: 17-0032-2010

53

DATUM: 28.04.2011.

VRIJEME: OD 13:45

DO

MATEMATIKA 1: Trajanje 100 minuta. Zabranjen je razgovor sa drugim studentima. ZADATKE RIJEŠAVATE

JEDNOSTRANO NA PAPIRE KOJE DOBIJETE OD NASTAVNIKA.

xoxo
Broj ↓
bodova

1. Odrediti determinantu matrice $A =$

$$\begin{bmatrix} 1 & 2 & 0 & 0 & 0 \\ 1 & 1 & 2 & 0 & 0 \\ 0 & 1 & 1 & 2 & 0 \\ 0 & 0 & 1 & 1 & 2 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix}$$

20

2. Odrediti domenu i sve asimptote funkcije $f(x) = x + \sqrt{x^2 + x + 1}$

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3. Ispitati konvergenciju reda $\sum \left(\frac{n^2 + 4n + 4}{2n + 2n^2} \right)^{2n}$

5

4. Ispitati domenu, periodičnost, parnost i prvu derivaciju funkcije $g(x) = \ln(\sin(3x))$.

11

5. Na temelju ispitivanja toka funkcije napraviti skicu grafa funkcije $h(x) = \frac{x^2 + 2}{x^2 + 1}$.

10

$$A = \begin{bmatrix} +1 & 2 & 0 & 0 & 0 \\ -1 & 1 & 2 & 0 & 0 \\ 0 & 1 & 1 & 2 & 0 \\ 0 & 0 & 1 & 1 & 2 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} +1 & 2 & 0 & 0 \\ -1 & 1 & 2 & 0 \\ +0 & 1 & 1 & 2 \\ -0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} +2 & 0 & 0 & 0 \\ -1 & 1 & 2 & 0 \\ +0 & 1 & 1 & 2 \\ -0 & 0 & 1 & 1 \end{bmatrix} = -1 + 6 = 5 \checkmark$$

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$$\begin{bmatrix} +1 & 2 & 0 & 0 \\ -1 & 1 & 2 & 0 \\ +0 & 1 & 1 & 2 \\ -0 & 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 2 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} - \begin{bmatrix} 2 & 0 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} = 2(-1) - 1(-2) = -3 - 1(-2) = -3 + 2 = -1$$

$$\begin{bmatrix} 1 & 2 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix} - \begin{bmatrix} 2 & 0 \\ 1 & 1 \end{bmatrix} = \underbrace{1((1 \cdot 1) - (2 \cdot 1))}_{-1} - \underbrace{1((2 \cdot 1) - (0 \cdot 1))}_{-2} = (1 \cdot 2) - 1(2) = -1 - 2 = -3$$

$$\begin{bmatrix} 2 & 0 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} = 2 \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix} - \begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix} = 2 \underbrace{1((1 \cdot 1) - (2 \cdot 1))}_{-1} - \underbrace{1((0 \cdot 1) - (0 \cdot 1))}_{0} = 2(1 \cdot 2) = 2 \cdot (-1) = -2$$

$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 1 & 1 & 2 & 0 \\ 0 & 1 & 1 & 2 \\ 0 & 0 & 1 & 1 \end{bmatrix} = 2 \begin{bmatrix} 1 & 2 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} - 1 \begin{bmatrix} 0 & 0 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix}$$

$$= 2 \left(\underbrace{\begin{bmatrix} 1 & 1 & 2 \\ 1 & 1 & 2 \end{bmatrix}}_{-1} - \underbrace{\begin{bmatrix} 2 & 0 \\ 1 & 1 \end{bmatrix}}_{-2} \right) - 1 \left(\begin{bmatrix} 0 & 0 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} \right)$$

$$= 2 \left(\underbrace{(1-1)}_{-1} - \underbrace{(2-1)}_{-1} - 1 \left(\underbrace{(2-1)}_{-2} - \underbrace{(0-1)}_{-1} \right) \right) = -6$$

2. $f(x) = x + \sqrt{x^2 + x + 1}$

$D(f) = \mathbb{R}$ ✓

$$\lim_{x \rightarrow +\infty} x + \sqrt{x^2 + x + 1} \cdot \frac{x - \sqrt{x^2 + x + 1}}{x - \sqrt{x^2 + x + 1}} = \frac{x^2 - x^2 + x + 1}{x - \sqrt{x^2 + x + 1}} = \frac{x+1}{x - \sqrt{x^2 + x + 1}} \cdot \frac{x}{x}$$

$+\infty + \infty = +\infty$

$$= \frac{\frac{x}{x} + \frac{1}{x}}{\frac{x}{x} - \sqrt{\frac{x^2}{x^2} + \frac{x}{x^2} + \frac{1}{x^2}}} = \frac{1}{0} = +\infty \quad \checkmark$$

$$\lim_{x \rightarrow -\infty} x + \sqrt{x^2 + x + 1} \cdot \frac{x - \sqrt{x^2 + x + 1}}{x - \sqrt{x^2 + x + 1}} = -\infty \quad \times$$

VIDI ŠIKIĆ

$$\lim_{x \rightarrow \infty} \frac{x + \sqrt{x^2 + x + 1}}{x} \stackrel{/:x}{=} \lim_{\frac{x}{x} \rightarrow \infty} \frac{\frac{x}{x} + \sqrt{\frac{x^2}{x^2} + \frac{x}{x^2} + \frac{1}{x^2}}}{\frac{x}{x}} = \frac{1+1}{1} = 2 \quad k=2 \checkmark$$

$l=?$ VIDI ŠIKIĆ

$$\lim_{x \rightarrow \infty} x + \sqrt{x^2 + x + 1} \cdot \frac{x - \sqrt{x^2 + x + 1}}{x - \sqrt{x^2 + x + 1}} = \frac{x+1}{x - \sqrt{x^2 + x + 1}} + 2x \stackrel{/:x}{=} \frac{3x+1}{x - \sqrt{x^2 + x + 1}} \stackrel{/:x}{=} \frac{\frac{3x}{x} + \frac{1}{x}}{\frac{x}{x} - \sqrt{\frac{x^2}{x^2} + \frac{x}{x^2} + \frac{1}{x^2}}}$$

NITI JEDNA ASIMPTOTA
NIJE SASVIM ISPRAVNA

$$= 3 \quad y=3$$

7

4. $f(x) = \ln(\sin(3x))$

- funkcija je periodična s periodom 2π ~~X~~

- $f(x) = f(-x)$

$f(x) = f(x)$

- funkcija nije ni parna ni neparna \checkmark



$f'(x) = \ln(\sin(3x))$

$$= \frac{1}{\sin(3x)} \cdot \sin'(3x) \cdot (3x)'$$

11

$$= \frac{1}{\sin(3x)} \cdot \cos 3x \cdot 3 = \frac{3 \cos 3x}{\sin(3x)} \quad \checkmark$$

$D(f) = ?$

IME I PREZIME: Matjaž Pešarič

BROJ INDEKSA: 17-0032-2010

$$3. \sum \left(\frac{n^2 + 4n + 4}{2n + 2n^2} \right)^{2n}$$

$$\lim \left(\frac{n^2 + 4n + 4}{2n + 2n^2} \right)^{2n} = \lim \frac{n^2 + 4n + 4}{2n^2 + 2n} \cdot \frac{1}{n^2} = \lim \frac{\frac{n^2}{n^2} + \frac{4n}{n^2} + \frac{4}{n^2}}{\frac{2n^2}{n^2} + \frac{2n}{n^2}} = \left(\frac{1}{2} \right)^{2n} ?$$

-konvergira

ZASTO?

5

$$5. f(x) = \frac{x^2+2}{x^2+1}$$

$$D(f) = \mathbb{R}$$

$$f(0) = \frac{0^2+2}{0^2+1} = \frac{1}{2} //$$

$$T(0, \frac{1}{2})$$

$$0 = \frac{x^2+2}{x^2+1}$$

$$x^2+2=0$$

$$x^2=-2$$

$$x = \sqrt{2}$$

$$T(1,41, 0)$$

$$f'(x) = \frac{x^2+2}{x^2+1}$$

$$= \frac{(x^2+2)' \cdot (x^2+1) - (x^2+2) \cdot (x^2+1)'}{(x^2+1)^2}$$

$$= \frac{2x(x^2+1) - (x^2+2) \cdot 2x}{(x^2+1)^2}$$

$$= \frac{2x^2+2x-2x^2-4x}{(x^2+1)^2}$$

$$= \frac{-2x}{(x^2+1)^2} \Rightarrow \text{Amplajna pada?}$$

$$\frac{-2x}{(x^2+1)^2} = 0 \quad / \cdot (x^2+1)^2$$

$$-2x = 0$$

$$x = 0 \quad \checkmark$$

$$T(0,0)$$

10

VIDI ŠIKIĆ
MEDIC

$$\lim_{x \rightarrow \infty} \frac{x^2+2}{x^2+1} \quad / : x^2 = \frac{\frac{x^2}{x^2} + \frac{2}{x^2}}{\frac{x^2}{x^2} + \frac{1}{x^2}} = \frac{1 + \frac{2}{x^2}}{1 + \frac{1}{x^2}} = \frac{1}{1} = 1 \quad \checkmark$$

$$\lim_{x \rightarrow \frac{1}{1}} \frac{x^2+2}{x^2+1} = \frac{x^2+2}{x^3+x} \quad / : x^3 = \frac{\frac{x^2}{x^3} + \frac{2}{x^3}}{\frac{x^3}{x^3} + \frac{x}{x^3}} = \frac{\frac{1}{x} + \frac{2}{x^3}}{1 + \frac{1}{x^2}} = \frac{0}{1} = 0 \quad ?$$

