

Popunite odmah!

IME I PREZIME: BERNARDO KOTLAR

BROJ INDEKSA: 77-2-0075-2070

DATUM: 7.2.2017. VRIJEME: OD 12:20

DO 13:45

MATEMATIKA 1: Trajanje 100 minuta. Zabranjen je razgovor sa drugim studentima. ZADATKE RIJEŠAVATE

OXOO  
Broj ↓  
bodova

JEDNOSTRANO NA PAPIRE KOJE DOBIJETE OD NASTAVNIKA.

1. Koju relaciju zadovoljava inverz matrice? Provjeriti tu relaciju za inverz matrice (ako postoji)

$$A = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 1 & 0 & 2 & 0 \\ 0 & 2 & 0 & 1 \\ 2 & 0 & 1 & 0 \end{bmatrix}$$

2. Među kompleksnim brojevima odrediti  $\sqrt[4]{\frac{3+2i}{2-3i}}$

3. Zadana je funkcija  $f(x) = e^x$  i funkcija  $g(x) = \frac{-1}{x^2}$ . Odrediti domenu i sve asimptote funkcije  $h(x) = f(g(x))$ .

4. Ispitati domenu i drugu derivaciju funkcije  $S(x) = \ln\left(\frac{x+1}{x-1}\right)$ .

5. Na temelju ispitivanja toka napraviti skicu grafa funkcije  $S(x)$  iz zadatka 4.

UKUPNO

13



2.  $\sqrt[4]{\frac{3+2i}{2-3i}}$  ~~...~~  $r = \sqrt{x^2 + y^2}$

~~...~~

~~...~~

~~...~~

~~...~~

$\sqrt[4]{\frac{3+2i}{2-3i} \cdot \frac{2+3i}{2+3i}}$

$\sqrt[4]{\frac{6+9i+4i-6}{4+9}}$

$\sqrt[4]{\frac{13i}{13}}$

$r = \sqrt{\left(\frac{13}{13}\right)^2}$

$r = \frac{13}{13} = 1$  ✓

$\text{tg } \rho = \frac{0}{13} = 0$

$\rho = 90^\circ$

$\rho = \frac{\pi}{2}$  ✓

$k=0$

$z_1 = \sqrt[4]{-1} = \left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right)$  ✗

$z_2 = \sqrt[4]{-1} = (\cos 0 + i \sin 0)$  ✗

$z_3 = 1 \cdot (1 + 0)$

$z_4 = 1$

$\text{Re } z_1 = 1 \quad \text{Im } z_1 = 0$

$z_1 = 1 \left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right)$

$= \cos \frac{\pi}{4} + i \sin \frac{\pi}{4}$

$= \dots$

$z_2 = 1 \left(\cos \frac{\pi+2\pi}{4} + i \sin \frac{\pi+2\pi}{4}\right)$

$= \cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4}$

$= \dots \quad \text{ITD.}$

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$k=1$

$$z_2 = 1 \cdot \left( \cos \frac{\frac{\pi}{2} \cdot 2k\pi}{4} + i \sin \frac{\frac{\pi}{2} \cdot 2k\pi}{4} \right)$$

$$z_2 = 1 \cdot \left( \cos \frac{\pi}{4} + i \sin \frac{\pi}{4} \right) \quad \times$$

$$z_2 = 1$$

$$\operatorname{Re} z_2 = 1$$

$$\operatorname{Im} z_2 = 0$$

$k=2$

$$z_3 = 1 \cdot \left( \cos \frac{\frac{\pi}{2} \cdot 4\pi}{4} + i \sin \frac{\frac{\pi}{2} \cdot 4\pi}{4} \right) \quad \times$$

$$= 1 \cdot \left( \cos \frac{\pi}{2} + i \sin \frac{\pi}{2} \right)$$

$$\operatorname{Re} z_3 = 0$$

$$\operatorname{Im} z_3 = 1$$

$k=3$

$$z_4 = 1 \cdot \left( \cos \frac{\frac{\pi}{2} \cdot 6\pi}{4} + i \sin \frac{\frac{\pi}{2} \cdot 6\pi}{4} \right) \quad \times$$

$$z_4 = 1 \cdot \left( \cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2} \right)$$

$$\operatorname{Re} z_4 = -1$$

$$\operatorname{Im} z_4 = 0$$

$$4. \quad f(x) = \ln\left(\frac{x+7}{x-7}\right)$$

$$f'(x) = \frac{1}{\frac{x+7}{x-7}} \cdot \left( \frac{(x+7)' \cdot (x-7) - (x+7) \cdot (x-7)'}{(x-7)^2} \right)$$

$$f'(x) = \frac{x-7}{x+7} \cdot \frac{x-7 - x+7}{(x-7)^2}$$

$$f'(x) = \frac{x-7}{x+7} \cdot \frac{-2}{(x-7)^2} \quad \checkmark$$

$$f''(x) = \frac{(x-7)' \cdot (x+7)' - (x-7) \cdot (x+7)'}{(x+7)^2} \cdot \frac{-2}{(x-7)^2} + \frac{x-7}{x+7} \cdot \frac{(-2)' \cdot (x-7)^2 - (-2) \cdot 2(x-7) \cdot (x-7)'}{(x-7)^4}$$

$$= \frac{x+7 - x+7}{(x+7)^2} \cdot \frac{-2}{(x-7)^2} + \frac{x-7}{x+7} \cdot \frac{4 \cdot x-7}{(x-7)^4}$$

$$= \frac{2}{(x+7)^2} \cdot \frac{-2}{(x-7)^2} + \frac{x-7}{x+7} \cdot \frac{4}{(x-7)^3} \quad \checkmark$$

13

DOMENA ?

$$\begin{vmatrix} 0 & 7 & 0 & 2 \\ 7 & 0 & 2 & 0 \\ 0 & 2 & 0 & 7 \\ 0 & 0 & 7 & 0 \end{vmatrix} \cdot (-2)$$

$$\begin{vmatrix} 0 & 7 & 0 & 2 \\ 7 & 0 & 2 & 0 \\ 0 & 2 & 0 & 7 \\ 0 & 0 & 7 & 0 \end{vmatrix}$$

$$(-7) \begin{vmatrix} 7 & 0 & 2 & 7 \\ 2 & 0 & 7 & 0 \\ 0 & 7 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$-7 \cdot (0 + 0 - 12) - (0 - 3 + 0)$$

$$-7 \cdot (-12 + 3) = 9$$

$$\det A = 9$$

para

$$\begin{vmatrix} 0 & -3 & 0 & 12 \\ 3 & 0 & 12 & 0 \\ 0 & 12 & 0 & -3 \\ 12 & 0 & -3 & 0 \end{vmatrix}$$

$$-7 \begin{vmatrix} 0 & 7 & 2 & 0 \\ 7 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$-7 \cdot (0 + 0 + 4) - (7 + 0 + 0)$$

$$-7 \cdot (3) = -3$$

$$0^2 \begin{vmatrix} 0 & 0 & 0 & 2 \\ 2 & 0 & 7 & 0 \\ 0 & 2 & 0 & 7 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$0 - (0 + 0 + 0) - (0 + 0 + 0)$$

$$0$$

$$0 \cdot \begin{vmatrix} 7 & 0 & 0 & 7 \\ 0 & 2 & 0 & 2 \\ 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$0 \cdot (0 + 0 + 0) - (0 + 0 + 0)$$

$$= 0$$

$$(-7^3) \begin{vmatrix} 7 & 0 & 7 & 7 \\ 0 & 0 & 0 & 0 \\ 2 & 7 & 0 & 7 \end{vmatrix}$$

$$-7(0 + 4 + 0) - (0 + 7 + 0)$$

$$-7 \cdot (7) = -49$$

$$(-2^5) \begin{vmatrix} 7 & 0 & 2 & 7 \\ 0 & 2 & 0 & 2 \\ 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$-32 \cdot (2 + 0 + 0) - (0 + 0 + 0)$$

$$-2 \cdot (-6) = 12$$

$$-7 \begin{vmatrix} 7 & 0 & 0 & 7 \\ 2 & 0 & 7 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$-7 \cdot (0 + 0 + 4) - (0 + 7 + 0)$$

$$-7 \cdot (3) = -3$$

$$0 \cdot \begin{vmatrix} 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 0 \\ 2 & 7 & 0 & 7 \end{vmatrix}$$

$$0 - (0 + 0 + 0) - (0 + 0 + 0)$$

$$-2 \begin{vmatrix} 0 & 7 & 2 & 0 \\ 0 & 2 & 0 & 2 \\ 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$-2 \cdot (0 + 2 + 0) - (0 + 0 + 0)$$

$$-2 \cdot (2) = -4$$

$$-7 \cdot \begin{vmatrix} 0 & 7 & 0 & 0 \\ 7 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$-7 \cdot (0 + 4 + 0) - (7 + 0 + 0)$$

$$= -13$$

$$-2 \begin{vmatrix} 0 & 0 & 0 & 0 \\ 7 & 2 & 0 & 2 \\ 2 & 7 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$$-2 \cdot (0 + 0 + 2) - (0 + 0 + 0)$$

$$-2 \cdot (2) = -4$$

$$-2 \cdot \begin{vmatrix} 7 & 0 & 2 & 0 \\ 0 & 2 & 0 & 2 \\ 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix} =$$

$$-2 \cdot (2 + 0 + 0) - (0 + 0 + 0)$$

$$= -4$$

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BROJ INDEKSA:

$$A^{-1} = \frac{1}{\det A} \cdot \begin{vmatrix} 0 & -3 & 0 & 12 \\ -3 & 0 & 12 & 0 \\ 0 & 12 & 0 & -3 \\ 12 & 0 & -3 & 0 \end{vmatrix}$$

$$A^{-1} = \begin{vmatrix} 0 & -\frac{3}{9} & 0 & \frac{12}{9} \\ -\frac{3}{9} & 0 & \frac{12}{9} & 0 \\ 0 & \frac{12}{9} & 0 & -\frac{3}{9} \\ \frac{12}{9} & 0 & -\frac{3}{9} & 0 \end{vmatrix} \quad \times$$

$$\left[ \begin{array}{cccc} 0 & -\frac{1}{3} & 0 & \frac{4}{3} \\ -\frac{1}{3} & 0 & \frac{4}{3} & 0 \\ 0 & \frac{4}{3} & 0 & -\frac{1}{3} \\ \frac{4}{3} & 0 & -\frac{1}{3} & 0 \end{array} \right] \quad \times$$

$$A^{-1} \cdot A = \begin{vmatrix} ? \\ ? \\ ? \\ ? \end{vmatrix}$$

PROVERA:

VIDI KERES

Popuniti odmah!

IME I PREZIME:

Filip Penjalov

DATUM:

VRIJEME: OD 14:00

DO

14:50

BROJ INDEKSA:

57144

13

MATEMATIKA 1: Trajanje 100 minuta. Zabranjen je razgovor sa drugim studentima. ZADATKE RIJEŠAVATE JEDNOSTRANO NA PAPIRE KOJE DOBIJETE OD NASTAVNIKA.

0x00  
Broj ↓  
bodova

1. Koju relaciju zadovoljava inverz matrice? Provjeriti tu relaciju za inverz matrice (ako postoji)

$$A = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 1 & 0 & 2 & 0 \\ 0 & 2 & 0 & 1 \\ 2 & 0 & 1 & 0 \end{bmatrix}$$



2. Među kompleksnim brojevima odrediti  $\sqrt[4]{\frac{3+2i}{2-3i}}$

3. Zadana je funkcija  $f(x) = e^x$  i funkcija  $g(x) = \frac{-1}{x^2}$ . Odrediti domenu i sve asimptote funkcije  $h(x) = f(g(x))$ .



4. Ispitati domenu i drugu derivaciju funkcije  $S(x) = \ln\left(\frac{x+1}{x-1}\right)$ .

13

5. Na temelju ispitivanja toka napraviti skicu grafa funkcije  $S(x)$  iz zadatka 4.

$$S(x) = \ln\left(\frac{x+1}{x-1}\right)$$



$$S'(x) = \frac{1}{\frac{x+1}{x-1}} \cdot \frac{1(x-1) - (x+1)1}{(x-1)^2}$$

$D_f \in \langle 0, +\infty \rangle$  X  
VIDI MARKO ĆULINA

$$S'(x) = \frac{1}{x+1} \cdot \frac{(x-1) - (x+1)}{(x-1)^2}$$

$$(x+1)(x-1) = x^2 - 1$$

$$x-1 - x-1 = -2$$

$$S'(x) = \frac{(x-1) - (x+1)}{x^2 - 1} = \frac{-2}{x^2 - 1}$$

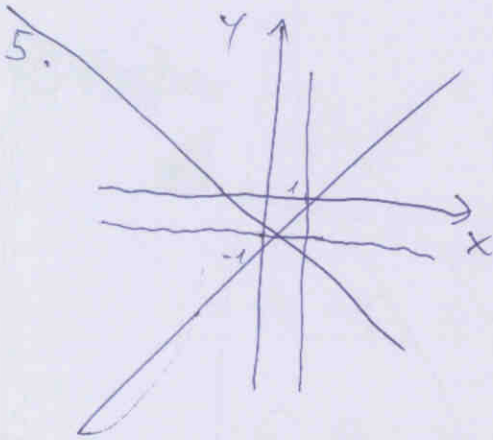
$$S'(x) = \frac{1}{x+1} - \frac{1}{x-1}$$

$$S'(x) = \frac{1}{x+1} - \frac{1}{x-1} \text{ ili } \boxed{S' = -\frac{2}{x^2-1}}$$

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$$S'' = -\frac{0 \cdot (x^2-1) - 2(2x)}{(x^2-1)^2} = -\frac{-4x}{(x^2-1)^2} = \frac{4x}{(x^2-1)^2} \text{ ili } \frac{4x}{x^4+2x+1}$$

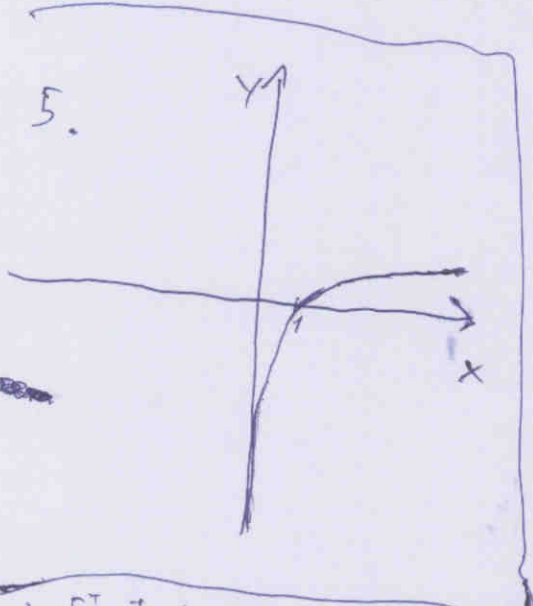
$$\frac{4x}{x^4} - \frac{2 \cdot 4x}{2x} + 4x = \frac{4}{x^3} - 2 + 4x = 2\left(\frac{2}{x^3} - 1 + 2x\right)$$



2.

$$z = \frac{4\sqrt{3+2i}}{2-3i}$$

$$|z| = 4\sqrt{2-3i}$$



3.  $f(x) = e^x$      $g(x) = -\frac{1}{x^2}$

$f(g(x))$

$$f(g(x)) = e^{-\frac{1}{x^2}}$$

1)

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 2 & 0 & 1 \\ 2 & 0 & 1 & 0 \end{pmatrix} \rightarrow -1 \begin{pmatrix} 1 & 2 & 0 \\ 0 & 0 & 1 \\ 2 & 1 & 0 \end{pmatrix} \rightarrow -2 \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 0 \\ 2 & 0 & 1 \end{pmatrix} \rightarrow -1 \left( 1 \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} - 2 \begin{pmatrix} 0 & 1 & 1 \\ 2 & 0 & 1 \end{pmatrix} \right) - 2 \left( 1 \begin{pmatrix} 2 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} + 2 \begin{pmatrix} 0 & 2 & 0 \\ 2 & 0 & 1 \end{pmatrix} \right)$$

$$\rightarrow -1(-1 - 4(-2)) - 2(2 + 2(-4)) = -1(3) - 2(0)$$

$$= -3$$



1)

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 2 & 0 & 1 \\ 2 & 0 & 1 & 0 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 2 & 0 \\ 0 & 0 & 1 \\ 2 & 1 & 0 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 0 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 0 & 2 & -1 \end{pmatrix}$$

$$\rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 0 & 0 & 2 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 0 & 2 & 0 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 0 & 0 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 2 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Popuniti odmah!

IME I PREZIME:

MARCO ČUINA

DATUM:

VRIJEME: OD

11:30

DO

12:30

BROJ INDEKSA:

1A-1-0008-2010

MATEMATIKA 1: Trajanje 100 minuta. Zabranjen je razgovor sa drugim studentima. ZADATKE RIJEŠAVATE JEDNOSTRANO NA PAPIRE KOJE DOBIJETE OD NASTAVNIKA.

0x00  
Broj ↓  
bodova

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~~0~~

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~~0~~

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~~0~~

5. Na temelju ispitivanja toka napraviti skicu grafa funkcije  $S(x)$  iz zadatka 4.

~~0~~

UKUPNO

~~0~~

0



$$A = \left[ \begin{array}{ccc|ccc} 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 \\ 1 & 0 & 2 & 0 & 0 & 1 & 0 & 0 \\ 0 & 2 & 0 & 1 & 0 & 0 & 1 & 0 \\ 2 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \end{array} \right] \sim \left[ \begin{array}{ccc|ccc} 1 & 0 & 2 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 \\ 0 & 2 & 0 & 1 & 0 & 0 & 1 & 0 \\ 2 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \end{array} \right] r_4 - 2r_1$$

$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 2 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 \\ 0 & 2 & 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & -1 & 0 & 0 & -2 & 0 & 1 \end{array} \right] r_3 - 2r_2 \quad \left[ \begin{array}{ccc|ccc} 1 & 0 & 2 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & -2 & 0 & 1 & 0 \\ 0 & 0 & -1 & 0 & 0 & -2 & 0 & 1 \end{array} \right] r_3 \leftrightarrow r_4$$

$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 2 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & -2 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & -2 & 0 & 1 & 0 \end{array} \right] \leftarrow 1/r_3 \quad \left[ \begin{array}{ccc|ccc} 1 & 0 & 2 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 2 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 & -2 & 0 & 1 & 0 \end{array} \right] r_1 - 2r_3$$

$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 1 & 0 & -1 & 0 & 2 \\ 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 2 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 & -2 & 0 & 1 & 0 & 0 \end{array} \right] \leftarrow 1/r_4 \quad \left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 1 & 0 & -1 & 0 & 2 \\ 0 & 1 & 0 & 2 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 2 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 2 & 0 & -1 & 0 & 0 \end{array} \right] r_2 - 2r_4$$

$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 1 & 0 & -1 & 0 & 2 \\ 0 & 1 & 0 & 0 & -3 & 0 & 2 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 2 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 2 & 0 & -1 & 0 & 0 \end{array} \right]$$

RELACIJA

$$A \cdot A^{-1} = I$$

OVA FUNKCIJA NEMA INVERZ ~~X~~

$$A \cdot A^{-1} = \left[ \begin{array}{ccc|ccc} 0 & 1 & 0 & 2 & 1 & 0 & -1 & 0 & 2 \\ 1 & 0 & 2 & 0 & -3 & 0 & 2 & 0 & 0 \\ 0 & 2 & 0 & 1 & 0 & 2 & 0 & -1 & 0 \\ 2 & 0 & 1 & 0 & 2 & 0 & -1 & 0 & 0 \end{array} \right]$$

$$\left[ \begin{array}{ccc|ccc} 0 & 1 & 0 & 2 & 1 & 0 & -1 & 0 & 2 \\ 1 & 0 & 2 & 0 & -3 & 0 & 2 & 0 & 0 \\ 0 & 2 & 0 & 1 & 0 & 2 & 0 & -1 & 0 \\ 2 & 0 & 1 & 0 & 2 & 0 & -1 & 0 & 0 \end{array} \right] \neq I \quad \text{VIDI KERES}$$

$$2) \sqrt[4]{\frac{3+2i}{2-3i}} = z$$

VIDI KOTLAR

$$\frac{3+2i}{2-3i} = \sqrt[4]{z}$$

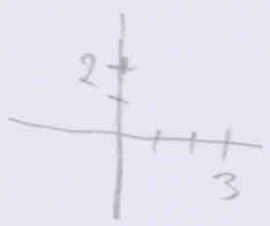
$$\frac{3+2i}{2-3i} = \sqrt[4]{z} / 2-3i$$

$$3+2i = \sqrt[4]{z} \times (2-3i)$$

$$\sqrt[4]{z} = 3+2i$$

$$r = \sqrt{x^2 + y^2} = \sqrt{3^2 + 2^2}$$

$$r = \sqrt{9+4} = \sqrt{13} = 3.60$$



$$\text{Re} = 3$$

$$\text{Im} = 2$$

$$\phi = \arcsin \frac{y}{x} = \arcsin \frac{2}{3} = 0.72$$

$$z_1 = \sqrt[4]{3.60} \left( \cos \frac{0.72 + 0.2\pi}{4} + i \sin \frac{0.72 + 0.2\pi}{4} \right) = 0.98 + i 0.17$$

$$z_2 = \sqrt[4]{3.60} \cdot (0.98 - 0.17i) = 1.34(0.98 + 0.17i) = 1.34 + 0.23i$$

$$z_3 = \sqrt[4]{3.60} \left( \cos \frac{0.72 + 1.2\pi}{4} + i \sin \frac{0.72 + 1.2\pi}{4} \right) = -0.17 + 0.98i$$

$$z_4 = 1.34(-0.17 + 0.98i) = -0.23 + 1.34i$$

$$z_5 = \sqrt[4]{3.60} \left( \cos \frac{0.72 + 2.2\pi}{4} + i \sin \frac{0.72 + 2.2\pi}{4} \right) = -0.98 - 0.17i$$

$$z_6 = 1.34(-0.98 - 0.17i) = -1.34 - 0.23i$$

$$z_7 = \sqrt[4]{3.60} \left( \cos \frac{0.72 + 3.2\pi}{4} + i \sin \frac{0.72 + 3.2\pi}{4} \right) = 0.17 - 0.98i$$

$$z_8 = 1.34(0.17 - 0.98i) = 0.23 - 1.34i$$

4

$$f(x) = \ln\left(\frac{x+1}{x-1}\right)$$

1 UVJET

2 UVJET

$$x-1 \neq 0$$

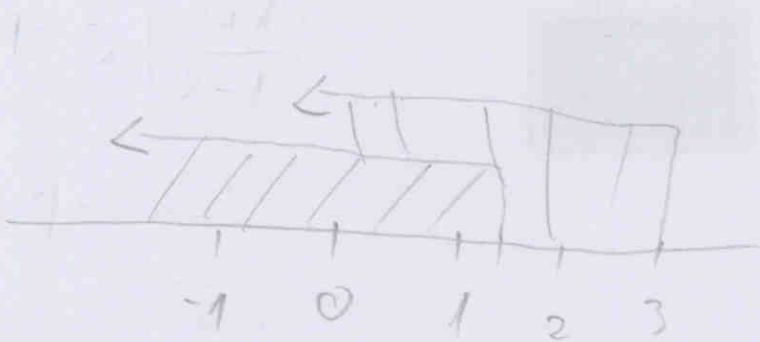
$$x \neq 1$$

$$-1 < \ln(x-1) < 1 \quad \text{ANTILOG} \quad \text{Df } x \in \mathbb{R} \setminus \{1\}$$

$$x-1 < 2.71 \quad x-1 < 0.36$$

$$x < 2.71+1 \quad x < 0.36+1$$

$$x < 3.71 \quad x < 1.36$$



$$\text{Df } \langle -\infty, 1.36 \rangle \cup \langle 3.71, +\infty \rangle \cup x \in \mathbb{R} \setminus \{1\}$$

$$D(\ln) = \langle 0, +\infty \rangle$$

$$\Rightarrow \frac{x+1}{x-1} \in \langle 0, +\infty \rangle \Rightarrow \frac{x+1}{x-1} > 0$$

NULTOČKA  $x_1 = -1$

NULTOČKA  $x_2 = 1$

	$-\infty$	$-1$	$1$	$+\infty$
$x+1$	-	+	+	
$x-1$	-	-	+	
$\frac{x+1}{x-1}$	(+)	-	(+)	

$$D(f) = \langle -\infty, -1 \rangle \cup \langle 1, +\infty \rangle$$

IME I PREZIME: MARKO ČULINA

BROJ INDEKSA:

$$S(x) = \ln\left(\frac{x+1}{x-1}\right)$$

$$S(x)' = \frac{1}{x}$$

$$S'(x) = \frac{\frac{1}{x}}{\left(\frac{x+1}{x-1}\right)} = \frac{x+1}{x-1} \times$$

~~0~~

VIDI PENJALOV

5)  $S(x) = \ln\left(\frac{x+1}{x-1}\right)$

VERTIKALNA ASIMPTOTA

$$\lim_{x \rightarrow 1} \ln\left(\frac{x+1}{x-1}\right) = \lim_{x \rightarrow 1} \ln\left(\frac{1+1}{1-1}\right) = \lim_{x \rightarrow 1} \ln\left(\frac{1}{0}\right) = +\infty$$

VERTICALNA ASIMPTOTA  $x=1$

HORIZONTALNA ASIMPTOTA

OVA FUNKCIJA NIJE PERIODIČNA ICR NO ŠAKOŠI  
TRIGONOMETRIJSKE FUNKCIJE

$f(x) \neq -f(x)$  } OVA FUNKCIJA NIJE NI  
 $-f(x) \neq f(-x)$  } PARNA NI NEPARNA

GRAF?